

# Level 2 Certificate in Further Mathematics June 2013 

Paper 2 8360/2

## Final

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## Glossary for Mark Schemes

These examinations are marked in such a way as to award positive achievement wherever possible. Thus, for these papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Mdep A method mark dependent on a previous method mark being awarded.

B dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent.
eg, accept 0.5 as well as $\frac{1}{2}$

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 1 | $r=5$ or $r^{2}=25$ or $r=\sqrt{25}$ or $\quad d=10$ | B1 | May be seen on diagram |
|  | ( $2 \times$ their $r)^{2}-\pi \times$ their $r^{2}$ | M1 |  |
|  | [21.45, 21.5] or $100-25 \pi$ | A1ft | ft from B0 M1 <br> Allow 21 with working (uses $25 \pi=79$ ) <br> Ignore any units seen |
| 2 (a) | $\frac{6}{3} \leq w<\frac{18}{3} \quad$ or $2 \leq w \ldots \ldots$ or ........ $w<6$ | M1 |  |
|  | $2 \leq w<6 \quad$ or $2 \leq w \leq 5$ | A1 |  |
|  | 2345 | A1ft | ft M1 A0 and inequality of form $a \leq w<b$ or $a \leq w \leq b$ <br> SC2 Answer 23456 or 345 with MO <br> SC1 Answer 691215 with M0 $\operatorname{SC} 1 \frac{6}{3}<w \leq \frac{18}{3}$ |
| 2 (b) | 16 | B1 |  |
| 2 (c) | their min from (a) - 3 | M1 |  |
|  | -1 | A1ft | ft their min from (a) |
| 3 (a) | $(5,0)$ | B1 | ( $5 x, 0 y$ ) is B0 <br> Check diagram for answer written next to $P$ if answer line is blank |
| 3 (b) | Correct elimination of a letter eg $2 x=15-3 x$ | M1 | $\text { oe eg } y=15-\frac{3}{2} y$ |
|  | Correctly collects terms <br> eg $2 x+3 x=15$ | M1dep | $\text { oe eg } y+\frac{3}{2} y=15$ |
|  | $(3,6)$ | A1 | Allow $x=3$ and $y=6$ if not contradicted on answer line |


| 3 (c) | $\frac{1}{2} \times$ their $5 \times$ their 6 | M1 | oe eg $\frac{2 \times 6}{2}+\frac{3 \times 6}{2}$ |
| :--- | :--- | :---: | :--- |
|  |  |  |  |


| 4 (a) | $\frac{2}{5} n \quad \text { or } \quad 0.4 n$ | B1 | oe |
| :---: | :---: | :---: | :---: |
|  | $(10 m=) 10 \times$ their $\frac{2}{5} n \quad(=4 n)$ | M1 | $10 \times 2(=20)$ and $3 \times 5(=15)$ |
| 4 (b) | 4:3 | A1ft | oe numerical ratio of integers ft their $\frac{2}{5} n$ if used |


| 5 | $25 x^{2}-15 x-15 x+9$ | M1 | 4 terms with 3 correct including a term in $x^{2}$ |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 25 x^{2}-15 x-15 x+9 \text { or } \\ & 25 x^{2}-30 x+9 \end{aligned}$ | A1 | Fully correct |
|  | Correctly differentiates their quadratic $\begin{array}{ll} 50 x-15-15 & \text { or } \\ 50 x-30 \end{array}$ | M1 | ft their $25 x^{2}-15 x-15 x+9$ |
|  | $\begin{aligned} & 10(5 x-3) \text { or } 5(10 x-6) \text { or } \\ & 2(25 x-15) \end{aligned}$ | A1ft | ft M1 A0 M1 if their $50 x-30$ factorises to $a(b x-c)$ where $a, b$ and $c$ are integers $>1$ |
|  | Alternative |  |  |
|  | $2(5 x-3) \times 5$ | M2 |  |
|  | $\begin{array}{lll} 10(5 x-3) & \text { or } 5(10 x-6) & \text { or } \\ 2(25 x-15) & & \end{array}$ | A2 |  |


| 6 (a) | $(c+4)(c+1)$ or $3(c+1)$ | M1 | Correct factorisation |
| :--- | :--- | :--- | :--- |
|  | $\frac{(c+4)(c+1)}{3(c+1)}=\frac{c+4}{3}$ | A1 | Must be a fraction and completed to $\frac{c+4}{3}$ |
|  | Correctly converts to a common <br> denominator <br> eg 1 $\frac{2(c+4)}{6}+\frac{3-2 c}{6}$ <br> eg 2 $\frac{6(c+4)}{18}+\frac{3(3-2 c)}{18}$ | M1 | M2 $\frac{2 c}{6}+\frac{8}{6}+\frac{3}{6}-\frac{2 c}{6}$ |


| 6 (b) | Correctly expands their brackets (must have common denominator) <br> $\frac{2 c+8+3-2 c}{6}$ or $\frac{2 c+8}{6}+\frac{3-2 c}{6}$ | M1 | Allow M1 if their first line of working is $\frac{2 c+4+3-2 c}{6} \text { or } \frac{2 c+4}{6}+\frac{3-2 c}{6}$ |
| :---: | :---: | :---: | :---: |
|  | $\frac{11}{6} \text { or } 1 \frac{5}{6} \text { or } 1.833(\ldots . .)$ | A1 | $\frac{33}{18} \mathrm{~A} 0 \quad \frac{5.5}{3} \mathrm{~A} 0 \quad \frac{8+3}{6} \mathrm{~A} 0$ |
|  | Alternative method |  |  |
|  | Correctly converts to a common denominator $\text { eg } \frac{6\left(c^{2}+5 c+4\right)}{6(3 c+3)}+\frac{(3-2 c)(3 c+3)}{6(3 c+3)}$ | M1 | oe <br> May also expand the denominator |
|  | Correctly expands their brackets (must have common denominator) $\begin{aligned} & \frac{6 c^{2}+30 c+24+9 c+9-6 c^{2}-6 c}{6(3 c+3)} \\ & \frac{6 c^{2}+30 c+24}{6(3 c+3)}+\frac{9 c+9-6 c^{2}-6 c}{6(3 c+3)} \end{aligned}$ | M1 | oe <br> May also expand the denominator |
|  | $\frac{11}{6}$ or $1 \frac{5}{6}$ or $1.833(\ldots)$. | A1 | $\frac{33}{18}$ A0 $\frac{5.5}{3} \mathrm{~A} 0 \quad \frac{8+3}{6} \mathrm{~A} 0$ |
| 7 | Scale on the $y$-axis identified correctly eg Intercept of line $A$ with $y$-axis identified as 2 | B1 | oe Must be unambiguous identification |
|  | Scale on the $x$-axis identified correctly eg Intercept of line $A$ with $x$-axis identified as 2 | B1 | oe Must be unambiguous identification |
|  | Correct attempt at gradient $\text { eg } \frac{\text { their } 5}{\text { their } 6}$ | M1 | ft their scales |
|  | $y=\frac{5}{6} x-5 \text { or } 6 y=5 x-30$ | A1ft | ft B0 B1 M1 or B1 B0 M1 oe $\frac{5}{6} x-5$ is B2 M1 A0 |


| $\mathbf{8 ~ ( a ) ~}$ | $y=-3$ or $\quad y+3=0$ | B 1 | Allow $y=0 x-3$ |
| :--- | :--- | :--- | :--- |
| $\mathbf{8 ( b )}$ | $x=1 \quad$ or $\quad x-1=0$ | B 1 |  |
| $\mathbf{8}(\mathbf{c})$ | $-2<x<1$ | B 1 | Unambiguously selected |


| 9 | (horizontal =) $8 \cos 42 \quad(=[5.9,6])$ or (horizontal =) $8 \sin 48 \quad(=[5.9,6])$ | M2 | M1 $\cos 42=\frac{x}{8}$ or $\sin 48=\frac{x}{8}$ ( $x$ is the horizontal) |
| :---: | :---: | :---: | :---: |
|  | $\begin{gathered} (\text { vertical }=) 8 \sin 42(=[5.35,5.4]) \text { or } \\ (\text { vertical }=) 8 \cos 48(=[5.35,5.4]) \text { or } \\ \text { (vertical }=) \sqrt{8^{2}-\text { their }[5.9,6]^{2}} \\ (=[5.35,5.4]) \end{gathered}$ | M2 | M1 $\sin 42=\frac{y}{8}$ or $\cos 48=\frac{y}{8}$ <br> ( $y$ is the vertical) <br> or <br> $8^{2}-$ their $[5.9,6]^{2}$ |
|  | [35.4, 35.5] | A1 |  |
|  | Alternative |  |  |
|  | $\begin{aligned} & (\text { vertical }=) 8 \sin 42 \quad(=[5.35,5.4]) \\ & (\text { vertical }=) 8 \cos 48(=[5.35,5.4]) \end{aligned}$ | M2 | M1 $\sin 42=\frac{y}{8} \quad$ or $\cos 48=\frac{y}{8}$ ( $y$ is the vertical) |
|  | $\begin{gathered} \text { (horizontal }=) 8 \cos 42(=[5.9,6]) \text { or } \\ \text { (horizontal=) } 8 \sin 48(=[5.9,6]) \text { or } \\ \text { (horizontal }=) \sqrt{8^{2}-\text { their }[5.35,5.4]^{2}} \\ (=[5.9,6]) \end{gathered}$ | M2 | M1 $\cos 42=\frac{x}{8}$ or $\sin 48=\frac{y}{8}$ <br> ( $x$ is the horizontal) <br> or <br> $8^{2}-$ their $[5.35,5.4]^{2}$ |
|  | [35.4, 35.5] | A1 | SC2 [31.8, 31.9] or |


| 10 | Straight line through ( $-3,0$ ) and $(0,3)$ | B1 | Lines must be ruled <br> Only penalise (by 1 mark) extended lines if B1 B1 B1 <br> SC2 Any graph that passes through $(-3,0)$ and $(0,3)$ and $(1,3)$ and $(2,1)$ |
| :---: | :---: | :---: | :---: |
|  | Straight line through (0,3) and (1, 3) | B1 |  |
|  | Straight line through (1,3) and (2,1) | B1 |  |
| 11 (a) | $\left(\begin{array}{cc}-a & 2 b-c \\ 0 & \frac{1}{3} b\end{array}\right)$ | B2 | B1 2 or 3 correct elements |
|  | $a=-1$ | B1ft | ft their matrix in (a) or if (a) correct ft their $b$ |
| 11 (b) | $b=3$ | B1ft |  |


| $c=6$ | B 1 ft |  |
| :--- | :--- | :--- | :--- |


| 12 | $5 n^{2}-5 n+3 n-3$ | M1 | oe 4 terms with 3 correct including a term in $n^{2}$ |
| :---: | :---: | :---: | :---: |
|  | $5 n^{2}-5 n+3 n-3$ | A1 | Fully correct <br> oe eg $5 n^{2}-2 n-3$ |
|  | $6 n^{2}-3$ | A1 |  |
|  | $3\left(2 n^{2}-1\right)$ or states that both terms are multiples of 3 | A1 | oe |


| 13 | Identifies (1, 3) or ( 5,11 ) | B1 | May be implied by M1 or seen in a table of values or on a graph or as a mapping (eg $1 \rightarrow 3$ ) |
| :---: | :---: | :---: | :---: |
|  | $\frac{\text { their } 11-\text { their } 3}{\text { their } 5-\text { their } 1} \quad(=2)$ | M1 | oe |
|  | $y-$ their $3=$ their $2(x-$ their 1$)$ or $y$ - their $11=$ their $2(x-$ their 5$)$ | M1 | $y=$ their $2 x+c$ and substitutes their $(1,3)$ or their $(5,11)$ |
|  | $(y=) 2 x+1$ | A1 |  |
|  | Alternative 1 |  |  |
|  | Identifies ( 1,11 ) or (5, 3) | B1 | May be implied by M1 or seen in a table of values or on a graph or as a mapping (eg $3 \rightarrow 1$ ) |
|  | $\frac{\text { their } 11-\text { their } 3}{\text { their } 1-\text { their } 5} \quad(=-2)$ | M1 | oe |
|  | $y$ - their $11=$ their $-2(x-$ their 1$)$ or $y-$ their $3=$ their $-2(x-$ their 5$)$ | M1 | $y=$ their $-2 x+c$ and substitutes their $(1,11)$ or their $(5,3)$ |
|  | $(y=)-2 x+13$ | A1 |  |
|  | Alternative 2 |  |  |
|  | $m+c=3$ or $5 m+c=11$ | B1 | $m+c=11$ or $5 m+c=3$ |
|  | Eliminates a letter from their 2 equations $\text { eg } \quad 5 m-m=11-3$ | M1 | Eliminates a letter from their 2 equations $\text { eg } \quad 5 m-m=3-11$ |
|  | $m=2$ or $c=1$ | A1 | $m=-2$ or $c=13$ |
|  | $(y=) 2 x+1$ | A1 | $(y=)-2 x+13$ |


| 14 | First and second differences correct $\begin{array}{lllll}\text { ie } & 4 & 6 & 8 & (10)\end{array}$ <br> 2 (2) | M1 |  |
| :---: | :---: | :---: | :---: |
|  | Correctly subtracts their $\frac{2}{2} n^{2}$ from given sequence <br> ie $\left.\begin{array}{lllll}10 & 11 & 12 & (13 & 14\end{array}\right)$ | M1 |  |
|  | (1) $n$ | M1dep | dep on M2 |
|  | $n^{2}+n+9$ | A1 | oe eg $n^{2}+n+10-1$ |
|  | Alternative method |  |  |
|  | $\begin{aligned} & \text { Any three of } \\ & a+b+c=11 \\ & 4 a+2 b+c=15 \\ & 9 a+3 b+c=21 \\ & 16 a+4 b+c=29 \\ & 25 a+5 b+c=39 \end{aligned}$ | M1 | Allow one error but each of their three equations must have $a, b$ and $c$ |
|  | Eliminates one variable to obtain a pair of equations in two variables <br> eg $3 a+b=4$ and $5 a+b=6$ | M1 | Allow one error |
|  | Eliminates one variable correctly eg $2 a=2$ | M1dep | dep on M2 |
|  | $n^{2}+n+9$ | A1 | oe eg $n^{2}+n+10-1$ |


| 15 (a) | $\frac{a^{9}(\times) b^{10}}{a^{11}(\times) b^{6}} \quad$ or $\quad a^{9-11}(x) b^{10-6}$ | M1 |  |
| :---: | :---: | :---: | :---: |
|  | $a^{-2}(x) b^{4} \quad \text { or } \quad \frac{b^{4}}{a^{2}}$ | A2 | A1 $a^{-2}$ or $b^{4}$ (M1 is implied) or $\left(\frac{b^{2}}{a}\right)^{2}$ or $\left(a^{-1}(x) b^{2}\right)^{2}$ SC1 $\quad a^{2}(\times) b^{-4}(\times c)$ |

15 (b)
$q^{-3}(x) r^{-2}$ or $\frac{1}{q^{3}(x) r^{2}}$
B2
B1 $q^{-3}$ or $r^{-2}$ or $\left(q^{6}(\times) r^{4}\right)^{-\frac{1}{2}}$ or $\left(q^{-6}(\times) r^{-4}\right)^{\frac{1}{2}}$ or $\frac{1}{\sqrt{q^{6}(\times) r^{4}}}$ or
$\sqrt{\frac{1}{q^{6}(\times) r^{4}}}$ or $\quad\left(q^{3}(\times) r^{2}\right)^{-1}$
or $p^{-1}=q^{3}(x) r^{2}$
or $\frac{1}{p}=q^{3}(\times) r^{2}$
or $p^{2}=q^{-6}(x) r^{-4}$
or $p^{2}=\frac{1}{q^{6}(\times) r^{4}}$

| 16 | Correct expressions or value for any three of these angles <br> angle $P A C=x$ <br> angle $C A B=90$ <br> angle $P B A=x$ <br> angle $P C A=180-2 x$ or $90+x$ <br> angle $A C B=90-x$ or $2 x$ <br> angle $C O A=2 x$ or $90-x$ <br> angle $P A O=90$ <br> angle $C A O=90-x$ or $2 x$ <br> angle $B A D=2 x$ or $90-x$ <br> angle $A O B=180-2 x$ or $90+x$ <br> angle $O A B=x$ | B3 | $O$ is the centre of the circle <br> $D$ is the point at the end of $P A$ extended <br> B2 Any 2 correct <br> B1 Any 1 correct |
| :---: | :---: | :---: | :---: |
|  | Writes a correct equation that has solution 30 <br> eg $1 P A C+C A B+x+P B A=180$ <br> eg $2 P C A+A C B=180$ <br> eg $3 A C B+C A B+C B A=180$ <br> eg $4 \quad P A O+A P C+P O A=180$ | M1 | oe |
|  | 30 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 17 | $\begin{aligned} & 4(x+3)+x-2 \text { or } \\ & \frac{4(x+3)}{(x-2)(x+3)}+\frac{x-2}{(x-2)(x+3)} \end{aligned}$ | M1 | Must be correct |
|  | $\left\{\begin{array}{l} 4 x+12+x-2 \quad(=5 x+10) \quad \text { or } \\ \frac{4 x+12}{(x-2)(x+3)}+\frac{x-2}{(x-2)(x+3)} \end{array}\right.$ | A1 |  |
|  | $5(x-2)(x+3)$ | M1 | Must have 5 and be correct <br> Must be in an equation and not a denominator <br> oe eg $(5 x-10)(x+3)$ |
|  | (5) $\left(x^{2}+3 x-2 x-6\right)$ | M1 | 5 may be missing <br> Must be in an equation and not a denominator <br> 4 terms including term in $x^{2}$ with 3 correct oe eg $1 x^{2}+x-6$ <br> eg $25 x^{2}+15 x-10 x-6$ (1 error) |
|  | $5 x^{2}=40$ | A1 | oe eg $5 x^{2}-40=0$ <br> Must collect all terms and have an equation |
|  | Correct attempt at solution of their quadratic $\text { eg } x=\sqrt{\frac{40}{5}}$ | M1dep | dep on M3 <br> Quadratic formula must have no errors in substitution <br> If completing square must have no errors up to $p(x-q)^{2}=r \quad p(x-q)^{2}-r=0$ |
|  | [2.8, 2.83] and [-2.83, -2.8] | A1ft | oe eg $(+) \sqrt{8}$ and $-\sqrt{8}$ or $\pm \sqrt{8}$ ft their quadratic equation if M4 <br> SC7 Both solutions correct (no valid method) SC3 One solution correct (no valid method) |


| 18 | $3 x^{2}+b$ | M1 | At least one term correct |
| :---: | :---: | :---: | :---: |
|  | Substitutes -2 into their $\frac{\mathrm{d} y}{\mathrm{~d} x}$ and equates to zero $3 \times(-2)^{2}+b=0$ | M1dep | Must have a term in $x$ $12+b=0$ |
|  | $b=-12$ | A1 |  |
|  | $(-2)^{3}+$ their $b(-2)+c=20$ | M1dep | dep on M2 and having a value for $b$ |
|  | $c=4$ | A1ft | ft their $b$ and M2 A0 M1dep with no errors in their final M1 |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 19 (a) | $\left[\begin{array}{ll} (12 \div 2)^{2}+4.5^{2} & \text { or } \\ 36+20.25 & \text { or } \\ 7.5^{2}-4.5^{2} & \text { or } \\ 7.5^{2}-6^{2} & \end{array}\right.$ | M1 | $4.5 \div 3(=1.5)$ and $6 \div 4(=1.5)$ |
|  | $\begin{aligned} & \sqrt{56.25}=7.5 \quad \text { or } \\ & \sqrt{36+20.25}=7.5 \text { or } \\ & \sqrt{6^{2}+4.5^{2}}=7.5 \text { or } \\ & 6^{2}+4.5^{2}=56.25 \text { and } 7.5^{2}=56.25 \text { or } \\ & \sqrt{20.25}=4.5 \quad \text { or } \\ & \sqrt{36}=6 \\ & \sqrt{7.5^{2}-4.5^{2}}=6 \quad \text { or } \\ & \sqrt{7.5^{2}-6^{2}}=4.5 \quad \text { or } \end{aligned}$ | A1 | $5 \times 1.5=7.5$ |
| 19 (b) | $\begin{aligned} & \tan M B N=\frac{3}{7.5} \\ & \sin M B N=\frac{3}{\sqrt{3^{2}+7.5^{2}}} \end{aligned} \quad \text { or } \quad \begin{aligned} & \cos M B N=\frac{7.5}{\sqrt{3^{2}+7.5^{2}}} \end{aligned}$ | M1 | Must be correct oe eg $\tan ^{-1} \frac{3}{7.5}$ |
|  | [21.8, 21.80141] | A1 |  |
| 19 (c) | $\begin{aligned} & \sin B N C=\frac{4.5}{7.5} \quad \text { or } \\ & \cos B N C=\frac{12 \div 2}{7.5} \quad \text { or } \\ & \tan B N C=\frac{4.5}{12 \div 2} \end{aligned}$ | M1 | $\begin{aligned} & \text { oe eg1 } \sin ^{-1} \frac{4.5}{7.5} \\ & \quad \text { eg } 2 \cos B N C=\frac{7.5^{2}+6^{2}-4.5^{2}}{2 \times 7.5 \times 6} \end{aligned}$ |
|  | [143, 143.1301024] | A1 | SC1 [36.8698976, 37] |
|  | Alternative 1 |  |  |
|  | $B D=\sqrt{12^{2}+4.5^{2}} \text { or } B D^{2}=12^{2}+4.5^{2}$ <br> and $\cos B N D=\frac{7.5^{2}+6^{2}-\text { their } B D^{2}}{2 \times 7.5 \times 6}$ | M1 |  |
|  | [143, 143.1301024] | A1 | SC1 [36.8698976, 37] |
|  | Alternative 2 |  |  |


| $\sin X N B=\frac{12 \div 2}{7.5}$ | $(=[53.1,53.13])$ or | M 1 | X is midpoint of AB |
| :--- | :--- | :--- | :--- | :--- |
| $\cos X N B=\frac{4.5}{7.5}$ | $(=[53.1,53.13])$ or |  |  |
| $\tan X N B=\frac{12 \div 2}{4.5}$ | $(=[53.1,53.13])$ |  |  |
| $[143,143.1301024]$ |  | A1 | SC1 $[53,53.1301024]$ |


| 20 | $\frac{1}{3}(x) \pi(x)(2 p)^{2}(x) 5 p \quad\left(=\frac{20 \pi}{3} p^{3}\right)$ | B1 | oe <br> Missing brackets B0 unless recovered <br> May be implied by working for M1 |
| :---: | :---: | :---: | :---: |
|  | their $\frac{1}{3}(x) \pi(x)(2 p)^{2}(x) 5 p=22500 \pi$ | M1 | oe eg $\frac{20 \pi}{3} p^{3}=22500 \pi$ <br> $\pi$ may already be cancelled or value for $\pi$ may be substituted in <br> Must be equating two volumes |
|  | Correctly rearranges to $p^{3}=$ eg $p^{3}=22500 \pi \div$ their $\frac{20 \pi}{3}$ | M1dep | oe eg $p=\sqrt[3]{3375}$ |
|  | 15 | A1 | SC3 [18.8, 18.9] |


| 21 | $2 a^{3}-7 a^{2}+3 a$ | M1 | Must be correct |
| :---: | :---: | :---: | :---: |
|  | $2 a^{2}-7 a+3$ | M1dep | Must be correct <br> May also see factor $a$ |
|  | $(2 a-1)(a-3)$ | A1 | May also see factor $a$ |
|  | 3 | A1ft | ft M1 M1 A0 <br> Other solutions may be seen but 3 must be selected as their answer |
|  | Alternative method |  |  |
|  | $(x-a)\left(2 x^{2}+2 a x-3\right)$ | M1 | Must be correct |
|  | $-3(x)-2 a^{2}(x)=-7 a(x)$ | M1dep | Equating coefficients of $x$ |
|  | $\begin{aligned} & 2 a^{2}-7 a+3 \text { and } \\ & (2 a-1)(a-3) \end{aligned}$ | A1 |  |
|  | 3 | A1ft | ft M1 M1 A0 <br> Other solutions may be seen but 3 must be selected as their answer |


| $\mathbf{Q}$ | Answer | Mark | Comments |
| :---: | :--- | :---: | :--- |
| $\mathbf{2 2}$ | $\tan \theta(\tan \theta+3)$ or $\tan \theta=0$ or <br> $\sin \theta(\sin \theta+3 \cos \theta)$ or $\sin \theta=0$ | M 1 | oe eg $t(t+3)$ <br> Must be correct |
|  | 180 | A 1 |  |
|  | $\tan \theta=-3$ | A 1 |  |
|  | $[108,108.44]$ | A 1 | B 1 ft |
| $[288,288.44]$ | $\mathrm{ft} 180+$ any angle (other than 0 and 90$)$ if <br> in range |  |  |


| 23 | Appropriate and correct sine rule in triangle $A B P$ <br> eg $\frac{B P}{\sin x}=\frac{A B}{\sin 30}$ | M1 | $\text { oe eg } \frac{B P}{A B}=\frac{\sin x}{\sin 30}$ |
| :---: | :---: | :---: | :---: |
|  | Appropriate and correct sine rule in triangle $A C P$ <br> eg $\frac{P C}{\sin x}=\frac{A C}{\sin 150}$ | M1 | oe eg $P C=\frac{\sin x}{\sin 150} \times A C$ |
|  | Eliminates $\sin x$ eg $\frac{P C}{\frac{B P \sin 30}{A B}}=\frac{A C}{\sin 150}$ | A1 | Must have M1 M1 oe eg $\frac{B P}{A B} \sin 30=\frac{P C}{A C} \sin 150$ |
|  | States $\sin 30=\sin 150$ | M1dep | dep on M1 M1 oe eg Substitutes $\sin 30=\frac{1}{2}$ and $\sin 150=\frac{1}{2}$ |
|  | Completes fully eg $\frac{P C}{A C}=\frac{B P}{A B}$ and $\quad \frac{A B}{A C}=\frac{B P}{P C}$ | A1 | Must have all 4 previous marks <br> SC1 Sine rule in triangle $A B P$ using angle $150-x$ <br> or <br> Sine rule in triangle $A C P$ using angle $30-x$ |

