

Centre Number										Candidate Number					
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Other Names															
Candidate Signature															



General Certificate of Education  
Advanced Subsidiary Examination  
June 2012

**Mathematics**

**MD01**

Unit Decision 1

Thursday 24 May 2012 9.00 am to 10.30 am

For this paper you must have:  
• the blue AQA booklet of formulae and statistical tables.  
You may use a graphics calculator.

**Time allowed**  
• 1 hour 30 minutes

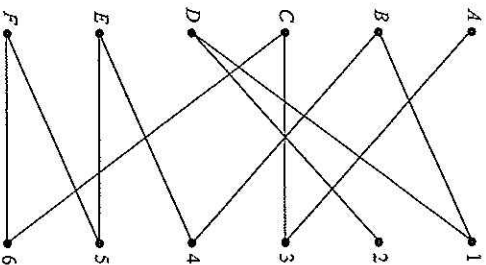
**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
  - Fill in the boxes at the top of this page.
  - Answer all questions.
  - Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
  - You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do not use the space provided for a different question.
  - Do not write outside the box around each page.
  - Show all necessary working; otherwise marks for method may be lost.
  - Do all rough work in this book. Cross through any work that you do not want to be marked.
  - The final answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Information**
- The marks for questions are shown in brackets.
  - The maximum mark for this paper is 75.
- Advice**
- You do not necessarily need to use all the space provided.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
<b>TOTAL</b>	

Answer all questions.  
Answer each question in the space provided for that question.

1 Six people, *A*, *B*, *C*, *D*, *E* and *F*, are to be allocated to six tasks, 1, 2, 3, 4, 5 and 6. The following bipartite graph shows the tasks that each of the people is able to undertake.



- (a) Represent this information in an adjacency matrix. (2 marks)
- (b) Initially, *B* is assigned to task 4, *C* to task 3, *D* to task 1, *E* to task 5 and *F* to task 6. By using an algorithm from this initial matching, find a complete matching. (3 marks)

QUESTION NUMBER	ANSWER SPACE
1	Answer space for question 1
	1 2 3 4 5 6
(a)	A 0 0 1 0 0 0
	B 1 0 0 1 0 0
	C 0 0 1 0 0 1
	D 1 1 0 0 0 0
	E 0 0 0 0 1 1
	F 0 0 0 0 0 1



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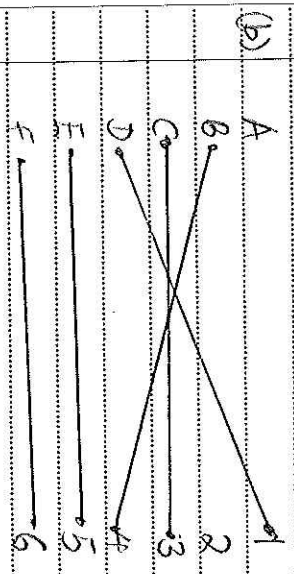
**MD01**



02

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QUESTION REFERENCE: Answer space for question 1



Complete matching

A - 3 = C

A - 3 = C - 6 - F - 5 = E - 4 = 8  
- 1 = D - 2

Match

A - 3 - C - 6 - F - 5 - E - 4 - 8

1 - D - 2

A 3, B 1, C 6, D 2, E 4, F 5

Turn over

QUESTION REFERENCE: 2 Answer space for question 2

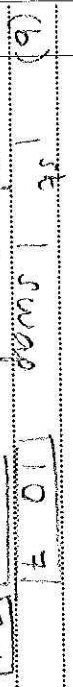
2 A student is using a shuttle sort algorithm to rearrange a set of numbers into ascending order.

Her correct solution for the first three passes is as follows.

Initial list	10	7	4	22	23	26
After 1st pass	7	10	4	22	23	26
After 2nd pass	4	7	10	22	23	26
After 3rd pass	4	7	10	22	23	26

- (a) Write down the number of comparisons on each of the three passes. (2 marks)
- (b) Write down the number of swaps on each of the three passes. (2 marks)
- (c) Explain whether or not the student has completed the algorithm. (1 mark)

(a) 1st 1 comparison  
2nd 2 comparisons  
3rd 1 comparison



2nd 2 swaps  
3rd no swaps.

(c) No, they have to check 23 and 26

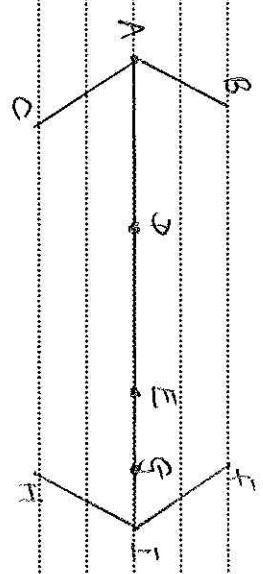




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QUESTION 3  
Answer space for question 3

(i) length = 97



b  
(i) 14

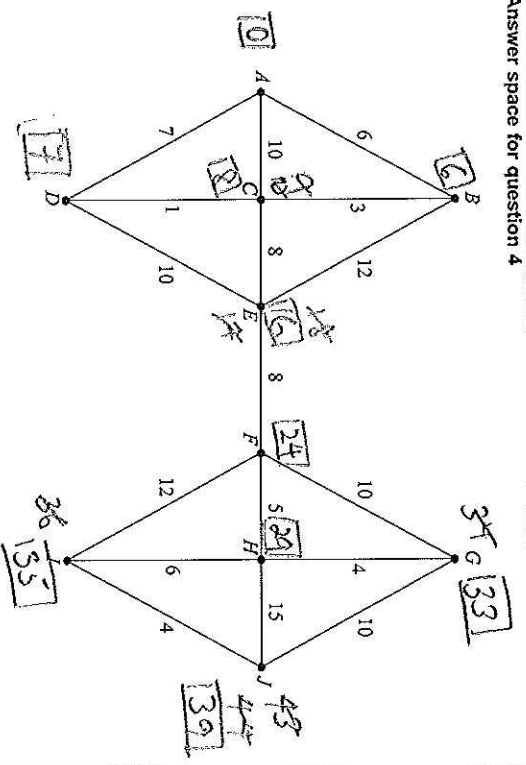
(ii) AC

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QUESTION 4  
Answer space for question 4

(a)(i)



(ii) A D C E F H J

(b) A - J => 39 minutes

$$\frac{39 \times 90}{60} = 58.5 \text{ km}$$

4 The edges on the network below represent some major roads in a city. The number on each edge is the minimum time taken, in minutes, to drive along that road.

(a) (i) Use Dijkstra's algorithm on the network to find the shortest possible driving time from A to J. (5 marks)

(ii) Write down the corresponding route. (1 mark)

(b) A new ring road is to be constructed connecting A to J directly. (2 marks)

Find the maximum length of this new road from A to J if the time taken to drive along it travelling at an average speed of 90 km/h, is to be no more than the time found in part (a)(i).



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QUESTION PART REFERENCE  
Answer space for question 5

length =  $2430 + 380$   
=  $2810$

(b)  $2430 + DF = 2430 + 340$   
=  $2770$

(c)  
(i)  $2430 + DH = 2430 + 180$   
=  $2610$

(ii) B and F only

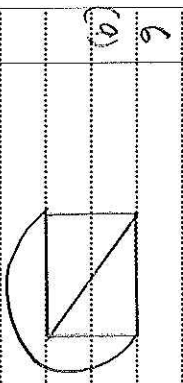
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QUESTION PART REFERENCE  
Answer space for question 6

6 The complete graph  $K_n$  ( $n > 1$ ) has every one of its  $n$  vertices connected to each of the other vertices by a single edge.

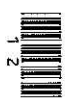
- (a) Draw the complete graph  $K_4$ . (1 mark)
- (b) (i) Find the total number of edges for the graph  $K_8$ . (2 marks)
- (ii) Give a reason why  $K_8$  is not Eulerian.
- (c) For the graph  $K_n$ , state in terms of  $n$ :
  - (i) the total number of edges;
  - (ii) the number of edges in a minimum spanning tree;
  - (iii) the condition for  $K_n$  to be Eulerian;
  - (iv) the condition for the number of edges of a Hamiltonian cycle to be equal to the number of edges of an Eulerian cycle. (4 marks)



(b) (i)  $K_8 = \frac{8(8-1)}{2} = \frac{8 \times 7}{2} = \frac{56}{2} = 28$

(ii) Odd number of edges at all vertices.

(c) (i) total number of edges  $\frac{n(n-1)}{2}$



QUESTION NUMBER: Answer space for question 6

(i)  $n-1$

(ii)  $n$  must be odd

(iv)  $n = 3$

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Rupra, a sales representative, has to visit six shops, A, B, C, D, E and F. Rupra starts at shop A and travels to each of the other shops once, before returning to shop A. Rupra wishes to keep her travelling time to a minimum.

The table shows the travelling times, in minutes, between the shops.

	A	B	C	D	E	F
A	-	16	10	25	26	40
B	16	-	20	19	18	50
C	10	20	-	14	22	31
D	25	19	14	-	11	32
E	26	18	22	11	-	42
F	40	50	31	32	42	-

- (a) Find the travelling time of the tour ACFDEBA. (1 mark)
- (b) Use the nearest neighbour algorithm, starting at A, to find an upper bound for the travelling time for Rupra's tour. (4 marks)
- (c) By deleting A, find a lower bound for the travelling time for Rupra's tour. (4 marks)
- (d) Sketch a network showing the edges that give you the lower bound in part (c) and comment on its significance. (2 marks)

QUESTION NUMBER: Answer space for question 7

(a) A C F D E B A  
 $10 + 31 + 32 + 11 + 18 + 16 = 118$

118.

(b) A C D E B F A  
 $10 \ 14 \ 11 \ 12 \ 50 \ 40$   
 $= 143$  (added together)



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QUESTION REFERENCE  
Answer space for question 8

(b) It would create a never-ending loop. A, B, C always repeat to 1.

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9 Oilyin is buying new pillows for his hotel. He buys three types of pillow: soft, medium and firm.

He must buy at least 100 soft pillows and at least 200 medium pillows.

He must buy at least 400 pillows in total.

Soft pillows cost £4 each. Medium pillows cost £3 each. Firm pillows cost £4 each.

He wishes to spend no more than £1800 on new pillows.

At least 40% of the new pillows must be medium pillows.

Oilyin buys  $x$  soft pillows,  $y$  medium pillows and  $z$  firm pillows.

(a) In addition to  $x \geq 0$ ,  $y \geq 0$  and  $z \geq 0$ , find five inequalities in  $x$ ,  $y$  and  $z$  that model the above constraints. (3 marks)

(b) Oilyin decides to buy twice as many soft pillows as firm pillows.

(i) Show that three of your answers in part (a) become

$$3x + 2y \geq 800$$

$$2x + y \leq 600$$

$$y \geq x$$

(3 marks)

(ii) On the grid opposite, draw a suitable diagram to represent Oilyin's situation, indicating the feasible region. (5 marks)

(iii) Use your diagram to find the maximum total number of pillows that Oilyin can buy. (2 marks)

(iv) Find the number of each type of pillow that Oilyin can buy that corresponds to your answer to part (b)(iii). (1 mark)

QUESTION REFERENCE  
Answer space for question 9

$$x \geq 100, y \geq 200$$

$$x + y + z \geq 400$$

$$4x + 3y + 4z \leq 1800$$

$$y \geq 40 \quad (x + y + z)$$

$$100$$

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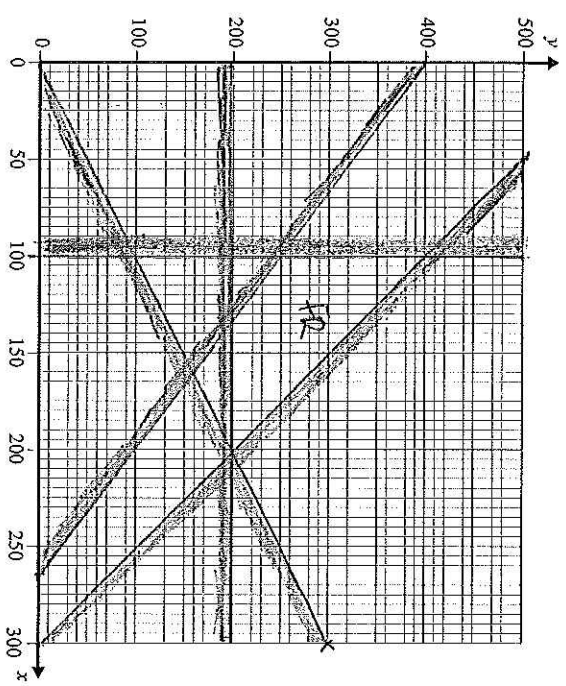


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QUESTION NUMBER: Answer space for question 9 (b)(ii)



(b) (i)  $x = 2 \Rightarrow 1x = 2$

$3x + y + 150 \leq 400$

$2x + y + x \leq 800$   
 $3x + y \leq 800$

$4x + 3y + 2x \leq 1800$   
 $6x + 3y \leq 1800$   
 $2x + y \leq 600$

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QUESTION NUMBER: Answer space for question 9

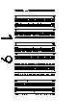
$5y \leq 2x + 2y + 2x$  (-2y both sides)  
 $3y \leq 4x$   
 $\therefore 3y \leq 4x$

(ii) maximum  $y + \frac{3}{2}x$   
 $400 + 150 = 550$

(iv) Ollie buys 100 soft, 400 medium and 50 firm pillows.

END OF QUESTIONS

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