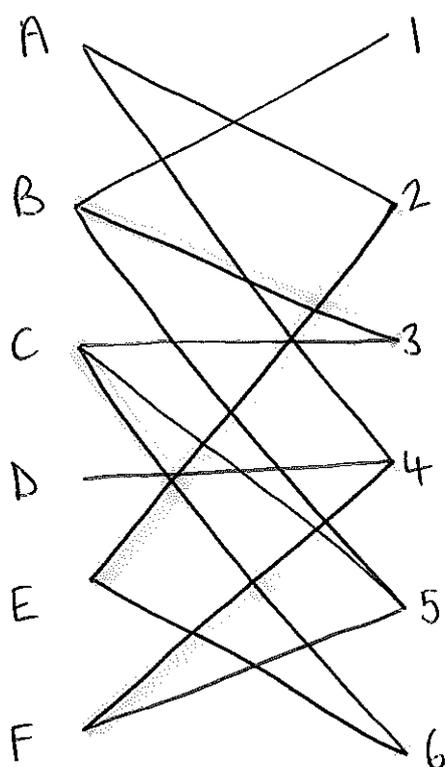


Jun '07

1a)



b) because D can only be matched to 4
so if F gets matched to 4 a complete
matching is impossible

c) $A-2 + E-6 + C-3 + B-1$

$D-4 + F-5$

A2

B1

C3

D4

E6

F5

2a)

28	22	20	17	14	11	6	5
28				14			
	22				11		
		20				6	
			17				5
14	11	6	5	28	22	20	17
14		6		28		20	
	11		5		22		17
6	5	14	11	20	17	28	22
5	6	11	14	17	20	22	28

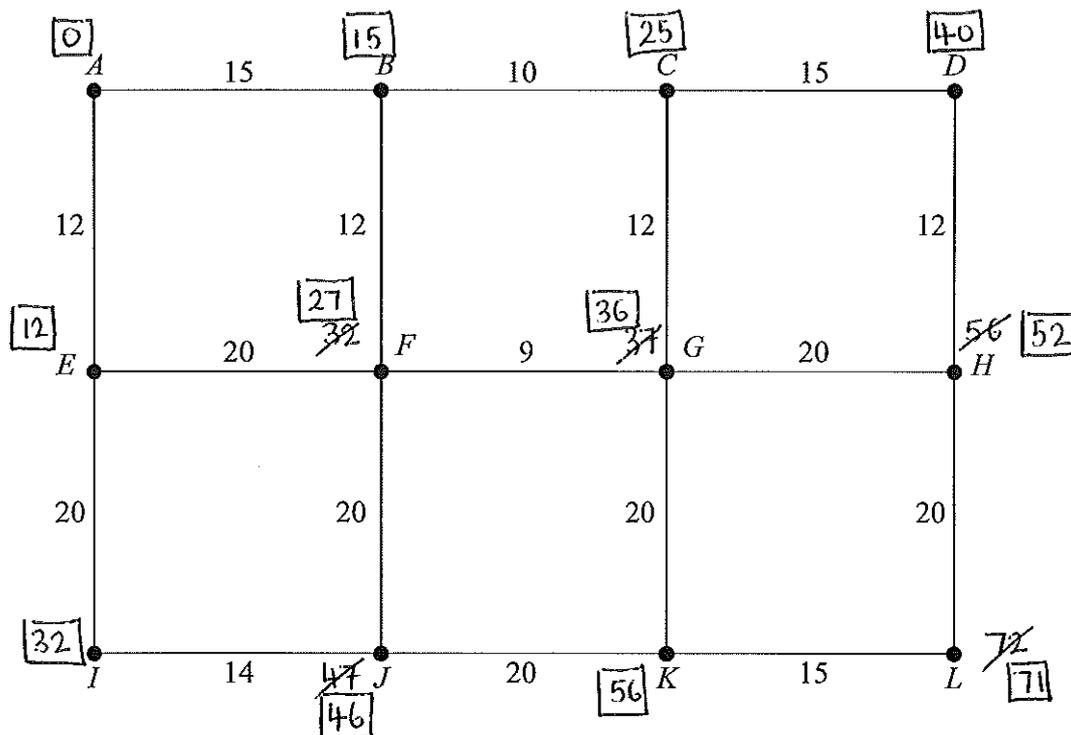
bi) Comparisons = 4

ii) Swaps = 4

c) $7 + 6 + 5 + 4 + 3 + 2 + 1 = 28$

3 [Figure 1, printed on the insert, is provided for use in this question.]

The following network represents the footpaths connecting 12 buildings on a university campus. The number on each edge represents the time taken, in minutes, to walk along a footpath.



- (a) (i) Use Dijkstra's algorithm on Figure 1 to find the minimum time to walk from A to L . (7 marks)
- (ii) State the corresponding route. (1 mark)
- (b) A new footpath is to be constructed. There are two possibilities:
- from A to D , with a walking time of 30 minutes; or
- from A to I , with a walking time of 20 minutes.

Determine which of the two alternative new footpaths would reduce the walking time from A to L by the greater amount. (3 marks)

Turn over ►

3 ai) see sheet 71 mins

ii) A B F G K L

b) $AD = 30 \rightarrow H \rightarrow L = 62$
12 20

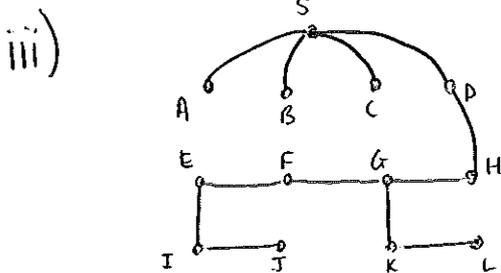
$AI = 20 \rightarrow J \rightarrow K \rightarrow L = 69$
14 20 15

New path AD by 9 mins

4ai)

SD	12
SC	13
SA	14
SB	16
DH	75
HG	23
GF	22
FE	24
EI	81
IJ	12
GK	83
KL	16
	<hr/>
	391

ii) 391



iv) FG 22
GH 23

b) odd vertices E, H, J, K

$$EH = 69 \text{ (EFGH)}$$

$$EJ = 93 \text{ (EIJ)}$$

$$EK = 129 \text{ (EFGK)}$$

$$JK = 131$$

$$HK = 106 \text{ (HGK)}$$

$$HJ = 142 \text{ (HGFJ)}$$

$$EH + JK = 69 + 131 = 200$$

$$EJ + HK = 93 + 106 = 199$$

$$EK + HJ = 129 + 142 = 271$$

$$1135 + 199 = 1334$$

5a) $5x + 10y \leq 1500 \Rightarrow x + 2y \leq 300$

$$32x + 8y \leq 4000 \Rightarrow 4x + y \leq 500$$

$$\left. \begin{array}{l} x \geq 50 \\ y \geq 50 \end{array} \right\} \begin{array}{l} \text{at least} \\ 50 \text{ of each} \end{array}$$

$$x + y \geq 140 \left\} \begin{array}{l} \text{at least} \\ 140 \text{ in total} \end{array}$$

bi) see next sheet

ii) $P = 0.8x + 1.2y$

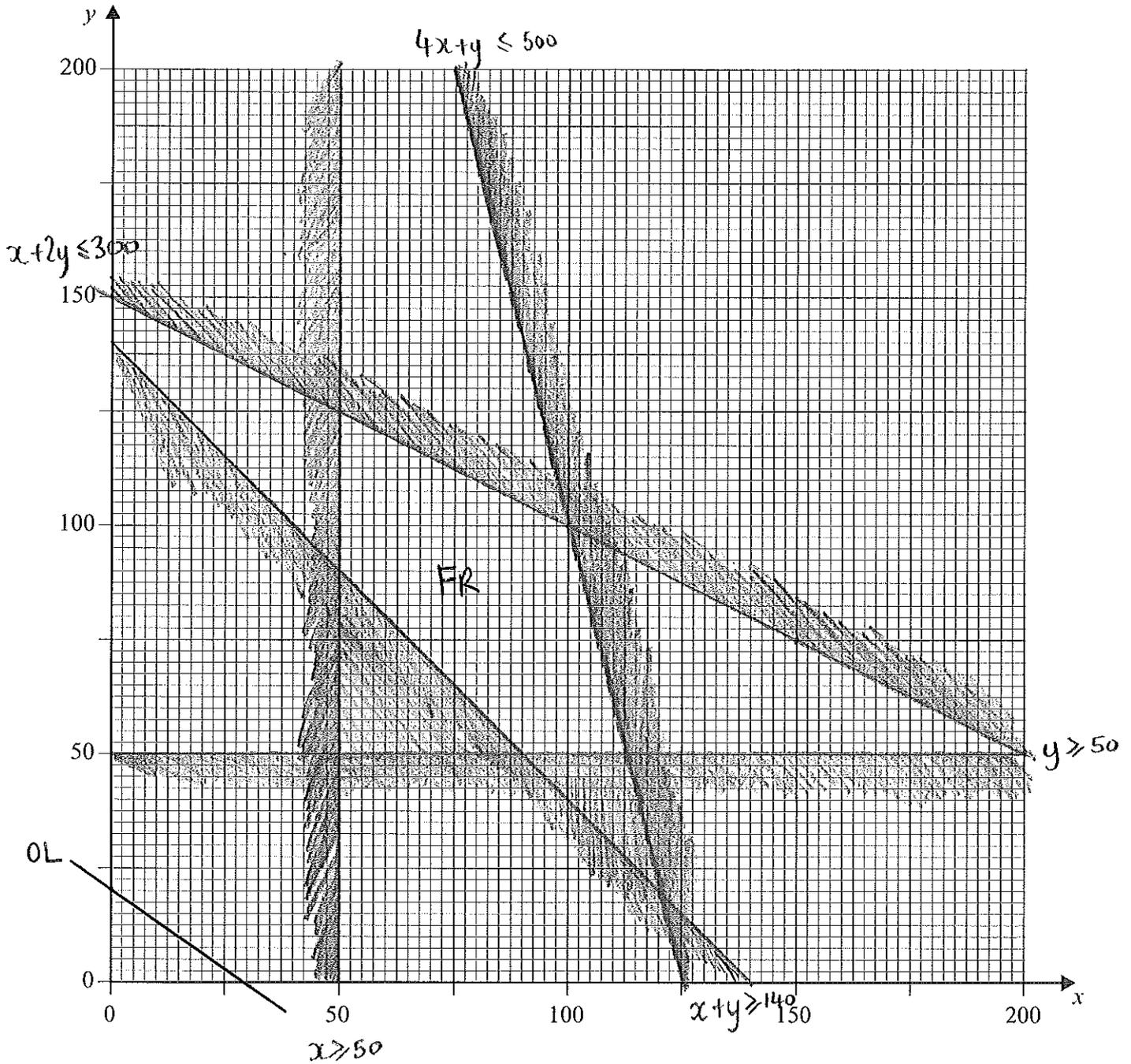
max at (100, 100)

$$\begin{aligned} P &= 0.8(100) + 1.2(100) \\ &= 80 + 120 = \pounds 200 \end{aligned}$$

iii) min at (90, 50)

$$\begin{aligned} P &= 0.8(90) + 1.2(50) \\ &= 72 + 60 = \pounds 132 \end{aligned}$$

Figure 2 (for use in Question 5)



$$P = 0.8x + 1.2y$$

$$240 = 8x + 12y$$

$$(0, 20) \quad (30, 0)$$

$$6ai) \quad G \rightarrow P \rightarrow A \rightarrow N \rightarrow R \rightarrow G$$

$$65 \quad 115 \quad 155 \quad 125 \quad 160 \quad = 620$$

$$ii) \quad \begin{array}{r} PA \quad 115 \\ RN \quad 125 \\ NA \quad 155 \\ \hline 395 \end{array} \quad \begin{array}{r} GP \quad 65 \\ GR \quad 160 \\ \hline 225 \end{array}$$

$$395 + 225 = 620$$

iii) As the upper and lower bound are the same, 620 must be the optimal solution.

$$bi) \quad G \rightarrow I \rightarrow M \rightarrow V \rightarrow G$$

$$20 \quad 32 \quad 21 \quad 19 \quad = 92$$

$$ii) \quad G \rightarrow V \rightarrow M \rightarrow I \rightarrow G$$

$$30 \quad 24 \quad 18 \quad 15 \quad = 87$$

$$iii) \quad 3 \times 2 \times 1 = 6$$

$$iv) \quad n!$$