Paper Reference(s)

1380/4H

Edexcel GCSE

Mathematics (Linear) – 1380

Paper 4 (Calculator)

Higher Tier

Friday 11 June 2010 – Morning

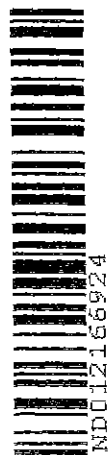Time: 1 hour 45 minutes

Materials required for examination	**Items included with question papers**
Ruler graduated in centimetres and millimetres, protractor, compasses, pen, HB pencil, eraser, calculator. Tracing paper may be used.	Nil

Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.
Check that you have the correct question paper.
Answer ALL the questions. Write your answers in the spaces provided in this question paper.
You must NOT write on the formulae page.
Anything you write on the formulae page will gain NO credit.
If you need more space to complete your answer to any question, use additional answer sheets.

Information for Candidates

The marks for individual questions and the parts of questions are shown in round brackets: e.g. **(2)**.
There are 27 questions in this question paper. The total mark for this paper is 100.
There are 24 pages in this question paper. Any blank pages are indicated.
Calculators may be used.
If your calculator does not have a π button, take the value of π to be 3.142 unless the question instructs otherwise.

Advice to Candidates

Show all stages in any calculations.
Work steadily through the paper. Do not spend too long on one question.
If you cannot answer a question, leave it and attempt the next one.
Return at the end to those you have left out.

Turn over

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Volume of a prism = area of cross section × length
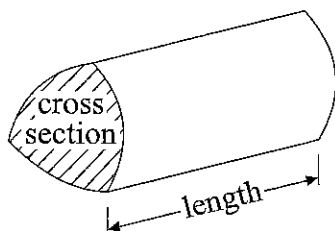
Volume of sphere $= \frac{4}{3}\pi r^3$

Surface area of sphere $= 4\pi r^2$
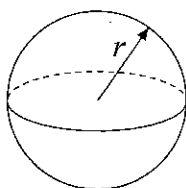
Volume of cone $= \frac{1}{3}\pi r^2 h$

Curved surface area of cone $= \pi r l$

In any triangle ABC

Sine Rule $\dfrac{a}{\sin A} = \dfrac{b}{\sin B} = \dfrac{c}{\sin C}$
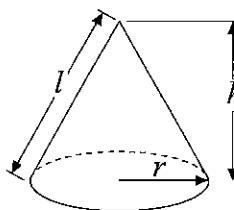
Cosine Rule $a^2 = b^2 + c^2 - 2bc \cos A$

Area of triangle $= \frac{1}{2} ab \sin C$
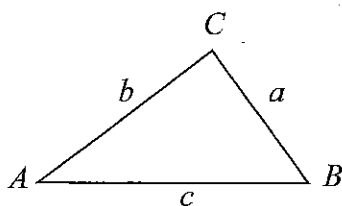
The Quadratic Equation

The solutions of $ax^2 + bx + c = 0$
where $a \neq 0$, are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$

N 3 6 7 6 2 A 0 2 2 4

Answer ALL TWENTY SEVEN questions.

Write your answers in the spaces provided.

You must write down all stages in your working.

1. Here is a list of ingredients for making a trifle for 4 people.

Trifle for 4 people
120 g of raspberry jelly
8 sponge fingers
420 m*l* of custard
180 g of tinned fruit

Rob is going to make a trifle for 6 people.
Work out the amount of each ingredient he needs.

Trifle for 2 people   ×3 → 6 people
60 Rasberry   180
4   Sponge   12
210 Custard   630
90 Fruit   270

..........180.......... g of raspberry jelly

..........12.......... sponge fingers

..........630.......... m*l* of custard
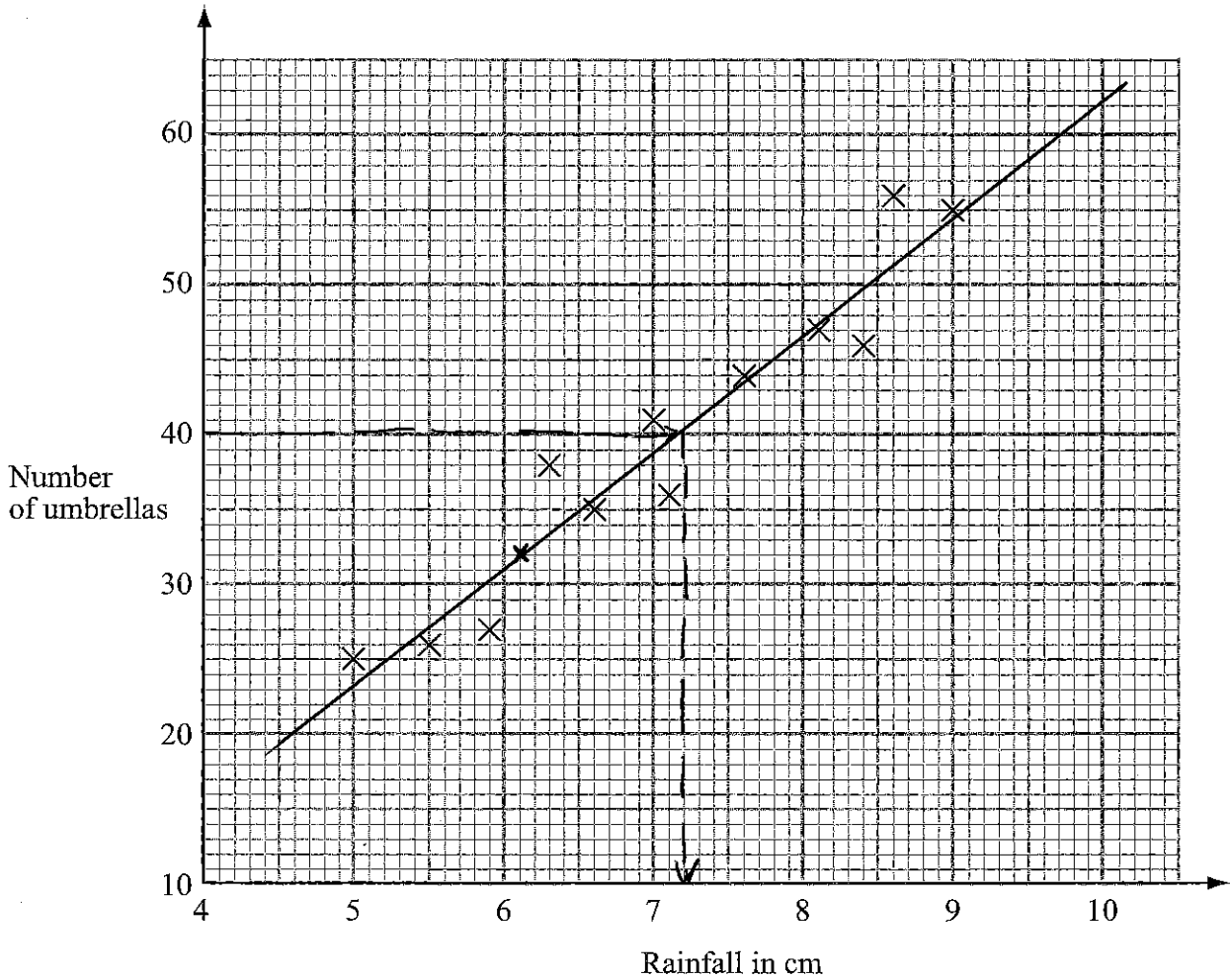
..........270.......... g of tinned fruit

(Total 3 marks)

Q1

2. Mr Wither sells umbrellas.

The scatter graph shows some information about the number of umbrellas he sold and the rainfall, in cm, each month last year.

In January of this year, the rainfall was 6.1 cm.
During January, Mr Wither sold 32 umbrellas.

(a) Show this information on the scatter graph.

(1)

(b) What type of correlation does this scatter graph show?

........Positive...correlation.........

(1)

In February of this year, Mr Wither sold 40 umbrellas.

(c) Estimate the rainfall for February.

.............7.2......... cm

(2)

(Total 4 marks)

3. In August 2008, Eddie hired a car in Italy.

The cost of hiring the car was £620
The exchange rate was £1 = €1.25

(a) Work out the cost of hiring the car in euros (€).

$620 \times 1.25 =$

€...........775...........

(2)

Eddie bought some perfume in Italy.

The cost of the perfume in Italy was €50
The cost of the same perfume in London was £42

The exchange rate was still £1 = €1.25

(b) Work out the difference between the cost of the perfume in Italy and the cost of the perfume in London.
Give your answer in pounds (£).

Italy: Perfume cost 50 ÷ 1.25 = £40

London: Perfume cost £42

Difference in cost = 42 - 40 = £2

£ ....2...........

(3)

Q3

(Total 5 marks)

4. (a) Complete the table of values for $y = 3x + 4$

x	-2	-1	0	1	2
y	-2	1	4	7	10

(2)

$x = -2 \qquad y = 3 \times -2 + 4 = -6 + 4 = -2$

Pattern $+3$

(b) On the grid, draw the graph of $y = 3x + 4$

$y = 3x + 4$

(2)

(Total 4 marks)

5.

112° (handwritten at top)
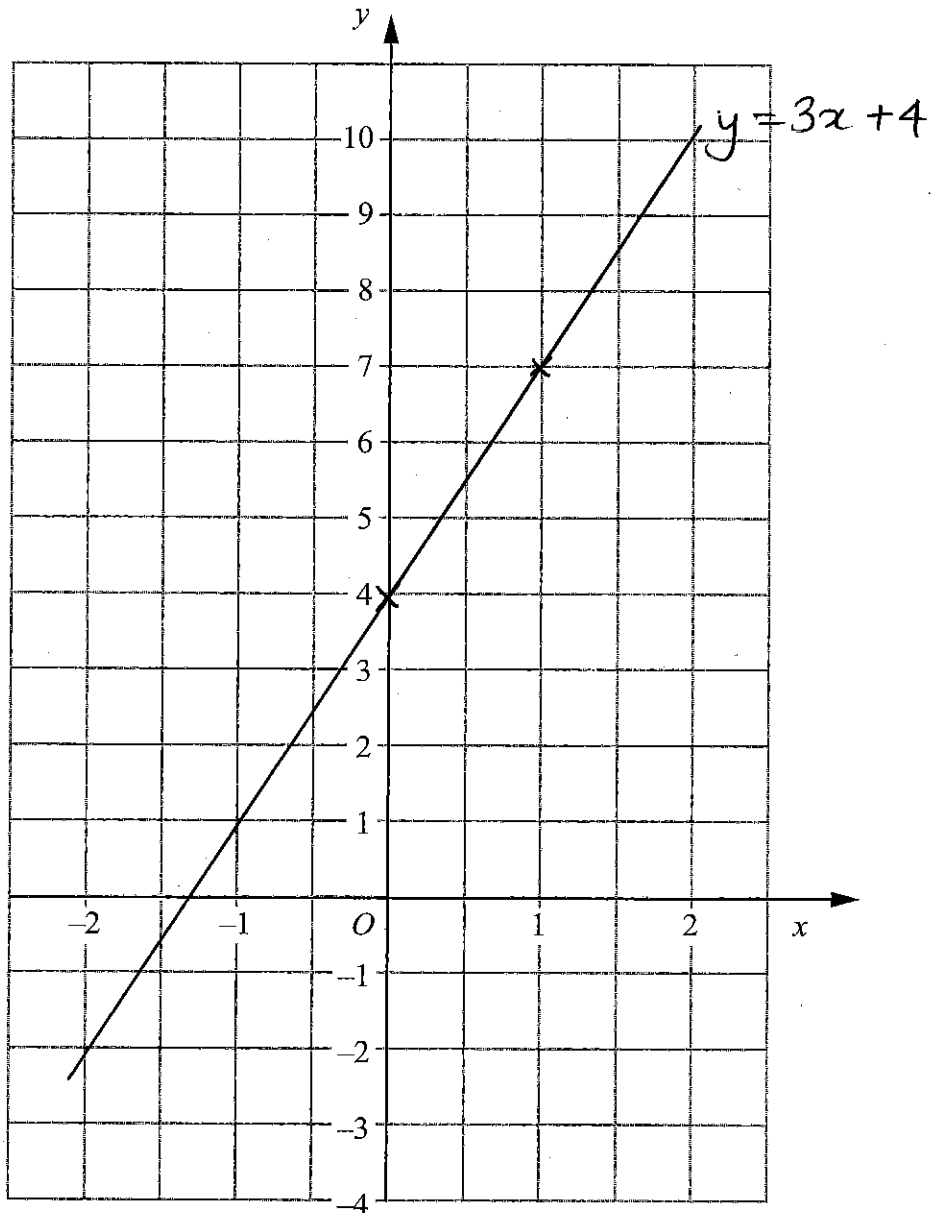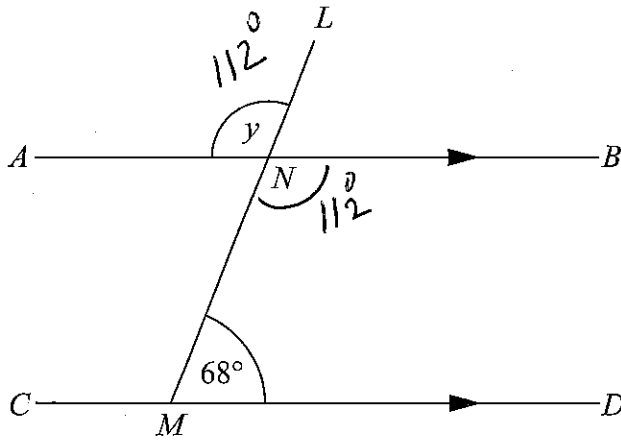
112° (handwritten near N)

ANB is parallel to *CMD*.
LNM is a straight line.
Angle *LMD* = 68°

$\angle MNB = 180 - 68 = 112°$

$y = 112$

(i) Work out the size of the angle marked *y*.

112 °

(ii) Give reasons for your answer.

— opposite angles are equal
— $\angle M$ & $\angle N$ Supplementary AB // CD

(Total 3 marks)

6. (a) Use your calculator to work out $\dfrac{2}{1.5 + 2.45}$

Write down all the figures on your calculator display.
You must give your answer as a decimal.

$2 \div (\ 1.5 \ + \ 2.45 \ ) \ =$

0.50632911

(2)

(b) Write your answer to part (a) correct to 2 decimal places.

0.51

(1)

(Total 3 marks)

7. A circle has a diameter of 12 cm.

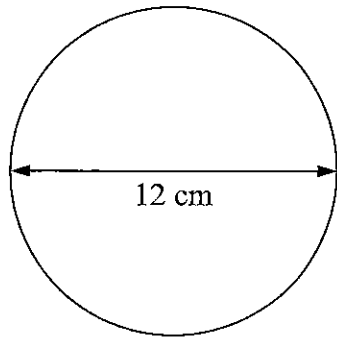Diagram **NOT**
accurately drawn

12 cm

$Circumference = 2\pi r$

$2r = d$

$C = \pi d$

$(r = radius \quad d = Diameter).$

Work out the circumference of the circle.
Give your answer correct to 3 significant figures.

$d = 12 cm$

$C = \pi \times d$

$C = \pi \times 12$

$C = 37.69911$

$37.7 \ (3sf)$ .... cm

Q7

(Total 2 marks)

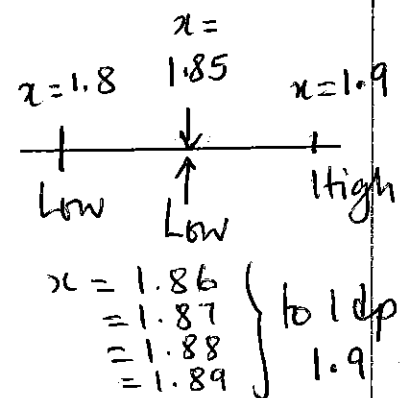**8.** The equation

$$x^3 + 10x = 25$$

has a solution between 1 and 2

Use a trial and improvement method to find this solution.
Give your answer correct to one decimal place.
You must show **all** your working.

x	$x^3 + 10x$	
1	$1^3 + 10 \times 1 = 11$	Low
2	$2^3 + 10 \times 2 = 28$	High
1.5	$1.5^3 + 10 \times 1.5 = 18.375$	Low
1.8	$1.8^3 + 10 \times 1.8 = 23.832$	Low
1.9	$1.9^3 + 10 \times 1.9 = 25.859$	High
1.85	$1.85^3 + 10 \times 1.85 = 24.8316$	Low

$x = 1.8 \quad 1.85 \quad x = 1.9$

Low   Low   High

$x = 1.86$
$= 1.87$ to 1 dp
$= 1.88$
$= 1.89$ 1.9

$x =$ .... 1.9 ....

Q8

(Total 4 marks)

9. Work out £84 as a percentage of £350

$$\frac{84}{350} \times 100 = 0.24 \times 100$$

.............24............ %

(Total 2 marks)

10. There are some ribbons in a box.
The ribbons are green or red or yellow or white.

The table shows each of the probabilities that a ribbon chosen at random will be green or red or white.

Colour	Green	Red	Yellow	White
Probability	0.15	0.30		0.35

(a) Work out the probability that a ribbon chosen at random will be yellow.

$P(\text{yellow}) = 1 - (0.15 + 0.30 + 0.35)$
$\qquad = 0.2$

......0.2......

(2)

There are 500 ribbons in the box.

(b) Work out the number of red ribbons.

$P(\text{red}) = 0.30$

Number of red ribbons $= 0.30 \times 500$

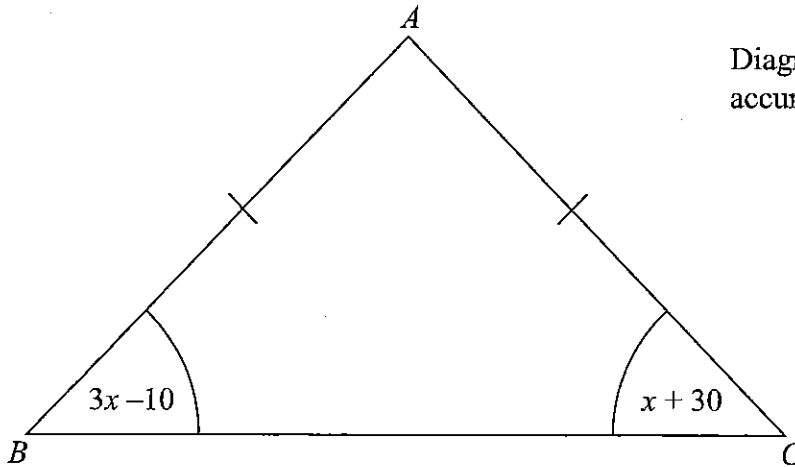......150 ribbons......

(2)

(Total 4 marks)

11.

Diagram **NOT** accurately drawn

ABC is an isosceles triangle.
AB = *AC*.

(a) Explain why $3x - 10 = x + 30$

$\triangle$ ABC iszreles, angles at the base are equal.
....

(1)

(b) Solve $3x - 10 = x + 30$

$$3x - x - 10 = x - x + 30$$
$$2x - 10 = 30$$
$$2x - 10 + 10 = 30 + 10$$
$$\frac{2x}{2} = \frac{40}{2}$$
$$x = 20$$

$x = $ ....**20**........

(2)   Q11

(Total 3 marks)

12.

Diagram **NOT** accurately drawn

6 cm

B   14 cm   *C*

ABC is a right-angled triangle.
AC = 6 cm.
BC = 14 cm.

$$\text{Area triangle} = \frac{base \times Height}{2}$$

(a) Work out the area of triangle *ABC*.

$$\text{Area} = \frac{14 \times 6}{2} = 42 \text{ cm}^2$$

....................**42**.................... cm^2

(2)

(b) Calculate the length of *AB*.
    Give your answer correct to 2 decimal places.

Pythagoras theoremen right angle triangle

$$AB^2 = BC^2 + AC^2$$
$$AB = \sqrt{14^2 + 6^2}$$
$$AB = \sqrt{232}$$
$$AB = 15.23 \ (2 dp)$$

....................**15.23**.................... cm

(3)

Q12

(Total 5 marks)

13. The diagram shows a solid prism.

Diagram **NOT**
accurately drawn

2 cm

1 cm

3 cm
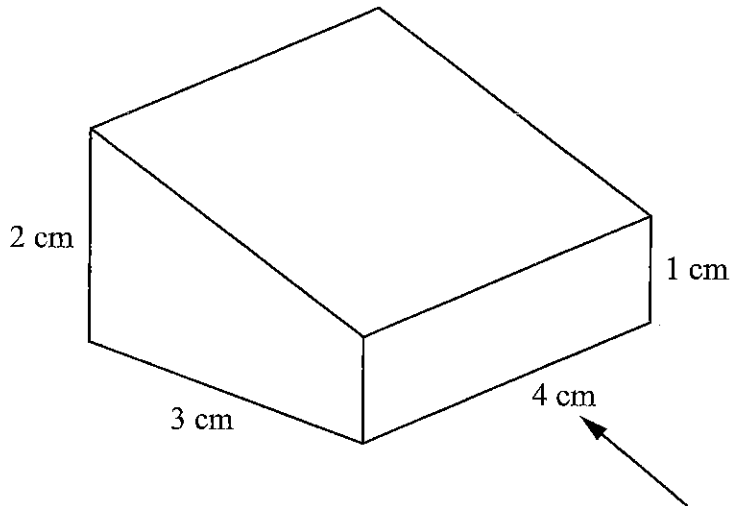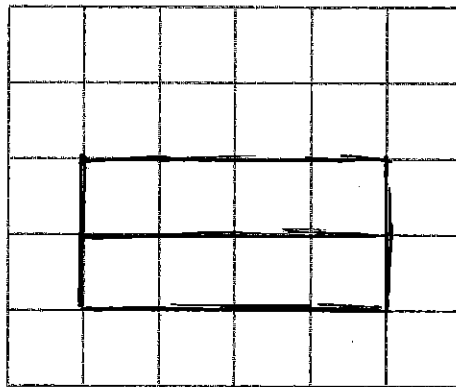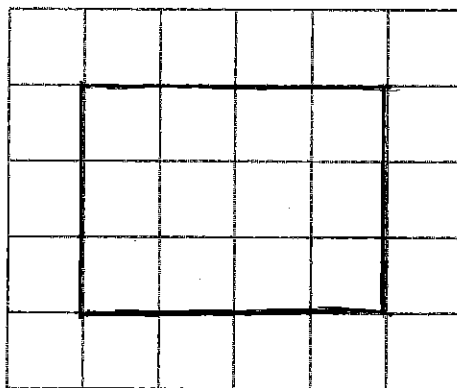
4 cm

(a) On the grid below, draw the front elevation of the prism from the direction of the arrow.

(2)

(b) On the grid below, draw the plan of the prism.

(2)

(Total 4 marks)

14. The table gives information about the number of CDs sold in a shop during each of the last 30 weeks.

Number of CDs (n)	Frequency	Midpoint	Total Frequency
$0 < n \leqslant 40$	3	20	3×20
$40 < n \leqslant 80$	5	60	5×60
$80 < n \leqslant 120$	12	100	12×100
$120 < n \leqslant 160$	7	140	7×140
$160 < n \leqslant 200$	3	180	3×180

Total = 30

Calculate an estimate for the mean number of CDs sold each week.
Give your answer correct to 1 decimal place.

$$\text{Mean} = \frac{\text{Total Number of CDs}}{\text{Frequency}}$$
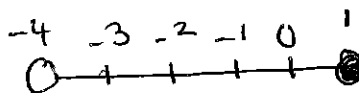
$$= \frac{3 \times 20 + 5 \times 60 + 12 \times 100 + 7 \times 140 + 3 \times 180}{30}$$

..........102.7 CDs..........

Q14

(Total 4 marks)

---

15. $-4 < n \leqslant 1$
n is an integer.

-4 -3 -2 -1 0 1

(a) Write down all the possible values of n.

..........$-3, -2, -1, 0, 1$..........

(2)

(b) Solve $3x - 2 > x + 7$

$3x - x - 2 > x - x + 7$

$2x - 2 > 7$

$2x - 2 + 2 > 7 + 2$

$2x > 9$

$x > 9/2$

or

$x > \dfrac{9}{2}$
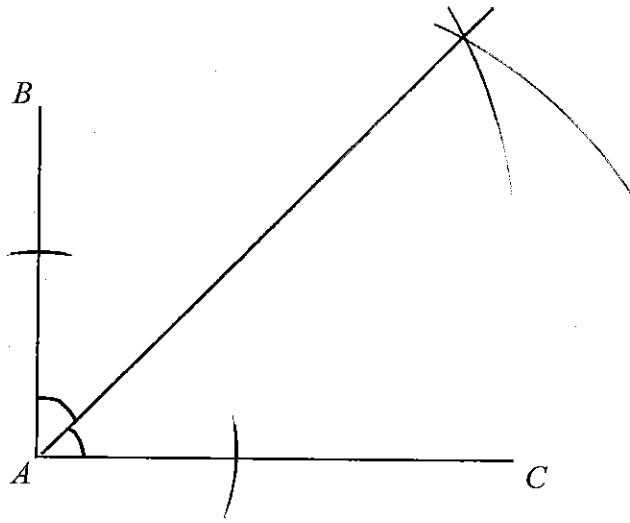
$x > 4.5$

(2)

Q15

(Total 4 marks)

Same distance.

16. Draw the locus of all points which are equidistant from the lines *AB* **and** *AC*.

The Locus of all points which are equidistant from lines AB and AC is the angle bisector.

Q16

(Total 2 marks)

17. Make *A* the subject of the formula

$$r = \sqrt{\frac{A}{3}} \quad \Longrightarrow \quad r^2 = \frac{A}{3}$$

$r^2 = \frac{A}{3}$ gives $3r^2 = A$

$A = \underline{\quad 3r^2 \quad}$

(Total 2 marks)

18. (a) Write 15 500 in standard form.

1.5×10^4

(1)

(b) Write 2.48×10^{-3} as an ordinary number.

2.48

0.00248

(1)

(c) Work out the value of

$$24\,500 \div (1.25 \times 10^{-4})$$

Give your answer in standard form. $24500 \div 0.000125$

Use calculator
$= 196\,000\,000$

1.96×10^8

(2)

(Total 4 marks)

19. (a) Factorise $x^2 - 7x + 10$

$$\begin{cases} ? + ? = -7 \\ ? \times ? = 10 \end{cases} \quad -2 ; -5$$

$(x - 2)(x - 5)$

$\underline{(x - 2)(x - 5)}$

(2)

(b) Solve $x^2 - 7x + 10 = 0$

$\Longleftrightarrow$

$(x - 2)(x - 5) = 0$

$x = 2$

or $x = 5$

$x = \underline{\quad 2 \quad}$

or $x = \underline{\quad 5 \quad}$

(1) **Q19**

(Total 3 marks)

20.

A

58°

16 m

C

B
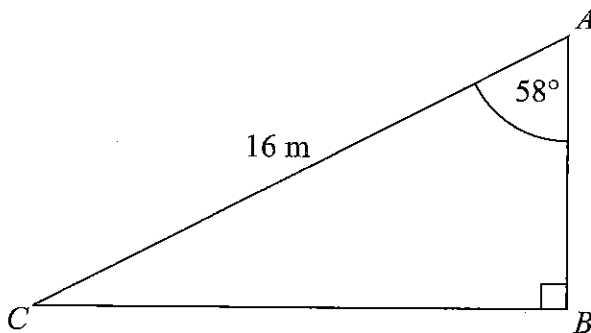
Diagram **NOT**
accurately drawn

SOH CAH TOA

$\cos 58 = \dfrac{AB}{16}$

ABC is a right-angled triangle.
AC = 16 m.
Angle *CAB* = 58°

Calculate the length of *AB*.
Give your answer correct to 3 significant figures.

$\cos 58 = \dfrac{AB}{16}$ gives $AB = 16 \cos 58°$

$AB = 8.47870$

$AB = 8.48 \ (3 \, Sf)$

$\underline{\quad 8.48 \quad}$ m

Q20

(Total 3 marks)

21. A field is in the shape of a rectangle.
The width of the field is 28 metres, measured to the nearest metre.

(a) Work out the upper bound of the width of the field.

$2\,8\cdot5$

.... metres

(1)

The length of the field is 145 metres, measured to the nearest 5 metres.

(b) Work out the upper bound for the perimeter of the field.

$U_b = 147.5$
$L_b = 142.5$

$L = (145 \pm 5/2)\,m \qquad 5/2 = 2.5$

$U_b\, P = (U_b \,Length + U_b\, Width) \times 2$

$= (147.5 + 28.5) \times 2$

352

.... metres

(3)

(Total 4 marks)

22. (a) Simplify $p^5 \times p^4$

p^{5+4}

p^9

.... **(1)**

(b) Simplify $q^5 \div q^2$

q^{5-2}

q^3

.... **(1)**

(c) Simplify $12tu^6 \div 6tu^5$

$\dfrac{\cancel{12}\ \cancel{t}u^6}{\cancel{6}\ \cancel{t}u^5} = 2u$

$2u$

.... **(2)**

(d) Simplify $(9w^2y^6)^{\frac{1}{2}}$

$= 9^{1/2}\, w^{2 \times 1/2}\, y^{6 \times 1/2}$

$= 3\, w\, y^3$

$3wy^3$

.... **(2)**

(e) For $x > 1$, write the following expressions in order of size.
Start with the expression with the least value.

$x^0 \qquad x^2 \qquad x \qquad x^{-2} \qquad x^{\frac{1}{2}}$

1

$x^{-2}\ x^0\ x^{1/2} \qquad x \qquad x^2$

$x^{-2} \quad x^0 \quad x^{1/2} \quad x \quad x^2$

.... **(2)**

(Total 8 marks)

Turn over

23. **A** and **B** are two solid shapes which are mathematically similar.
The shapes are made from the same material.

A

Diagram **NOT**
accurately drawn

B
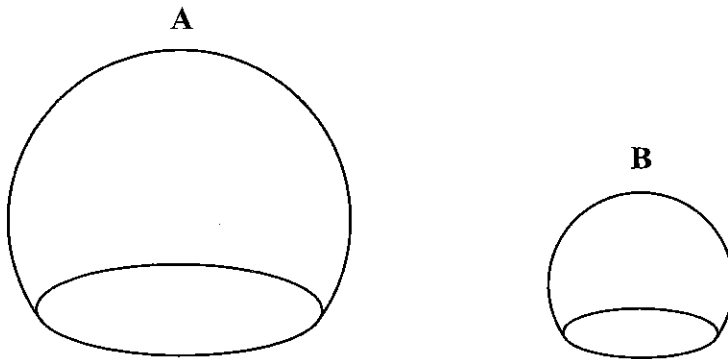
The surface area of **A** is 50 cm².
The surface area of **B** is 18 cm².

The mass of **A** is 500 grams.

Calculate the mass of **B**.

$$\text{Area } A = Sf^2 \times \text{Area } B$$

$$50 : 18$$
$$25 : 9 \leftarrow \text{Ratio of Area}$$
$$\text{Ratio of length } \sqrt{25} : \sqrt{9}$$
$$5 : 3$$
$$\text{Ratio of volume } 125 : 27$$

$$\text{Mass } A = Sf \times \text{Mass } B \quad \therefore \text{ Mass } B = \frac{\text{Mass } A}{Sf^3}$$

$$\text{Mass } B = \frac{500}{\frac{125}{27}} = 500 \times \frac{27}{125} = 108$$

.... 108 .... grams

Q23

(Total 4 marks)

24. (a) Explain what is meant by a random sample.

Each member of the population has an equal chance of selection –

(1)

Chris collects stamps from different countries.
He has 245 stamps from France.

He wants to take a random sample of 10 of his stamps from France.

(b) Describe a method that Chris could use.

○ Number each stamp & use random select on a calculator

○ Put stamps in a hat & pick

(1)

The table shows information about Chris' collection of 662 stamps.

Country	France	Germany	Spain	Italy	Total
Number of stamps	245	184	138	95	662

Chris takes a sample of 50 stamps stratified by country.

(c) Work out the number of stamps from Italy in this sample.

stamps Italy

$$\frac{95}{662} \times 50 = 7.175$$
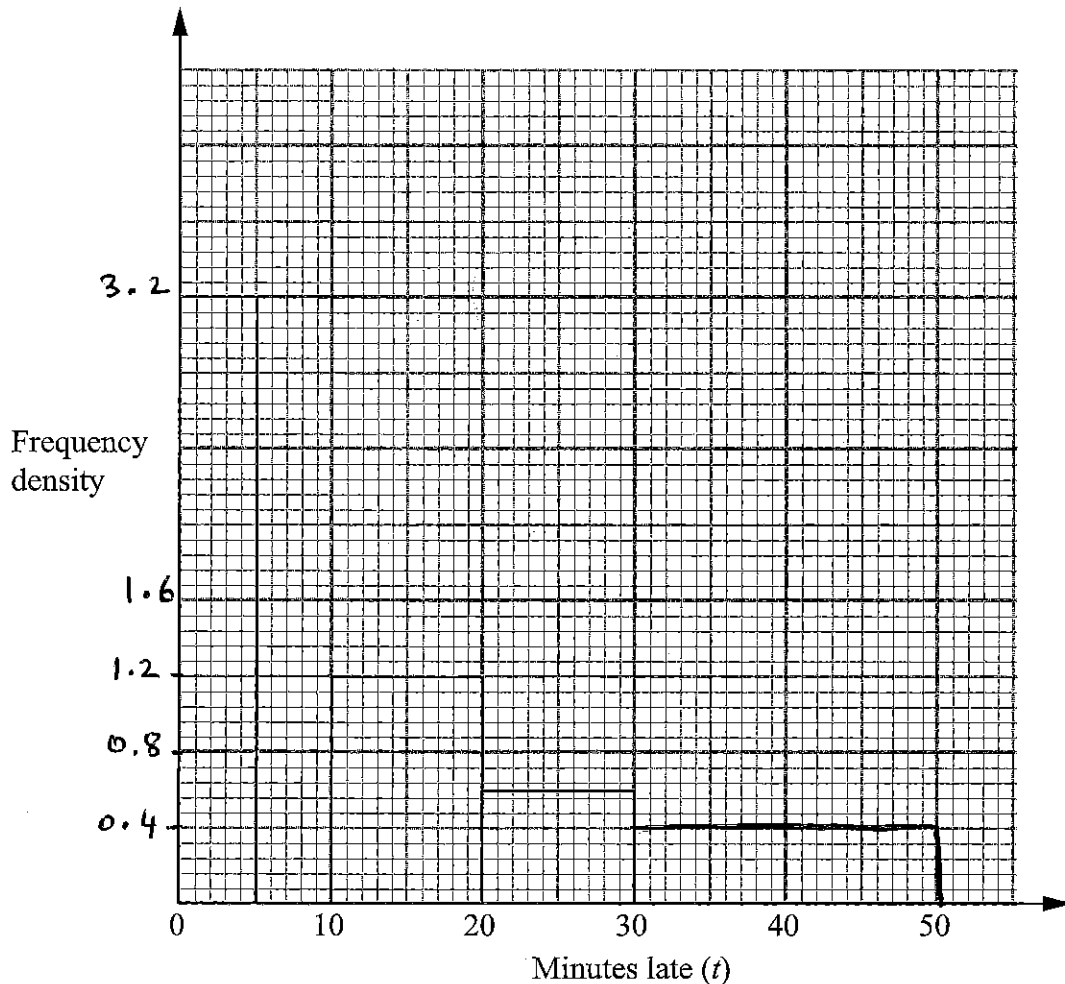
Total Number –

7

(2)

(Total 4 marks)

Q24

25. Some trains from Manchester to London were late.
The incomplete table and histogram gives some information about how late the trains were.

Minutes late (t)	Frequency
$0 < t \leqslant 5$	16
$5 < t \leqslant 10$	10
$10 < t \leqslant 20$	$1 \cdot 2 \times 10 = 12$
$20 < t \leqslant 30$	$0 \cdot 6 \times 10 = 6$
$30 < t \leqslant 50$	8

Fd

$16 \div 5 = 3 \cdot 2$

$8 \div 20 = 0 \cdot 4$

(a) Use the information in the histogram to complete the table.

(2)

(b) Use the information in the table to complete the histogram.

(2)

(Total 4 marks)

26. The diagram shows a sector of a circle with centre O.
The radius of the circle is 8 cm.

PRS is an arc of the circle.
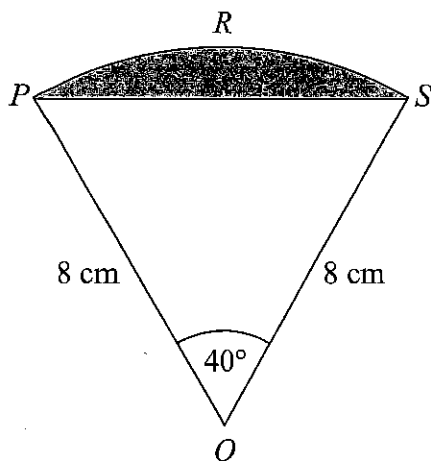PS is a chord of the circle.
Angle $POS = 40°$

Diagram **NOT**
accurately drawn

Calculate the area of the shaded segment.
Give your answer correct to 3 significant figures.

Area of shaded segment = Area of sector − Area of $\triangle$.

Area of sector = $\frac{40}{360} \times \pi \times 8^2$

Area of $\triangle OPS = \frac{1}{2} \times 8 \times 8 \sin 40°$

Area of segment = $\frac{40}{360} \times \pi \times 8^2 - \frac{1}{2} \times 8^2 \sin 40$
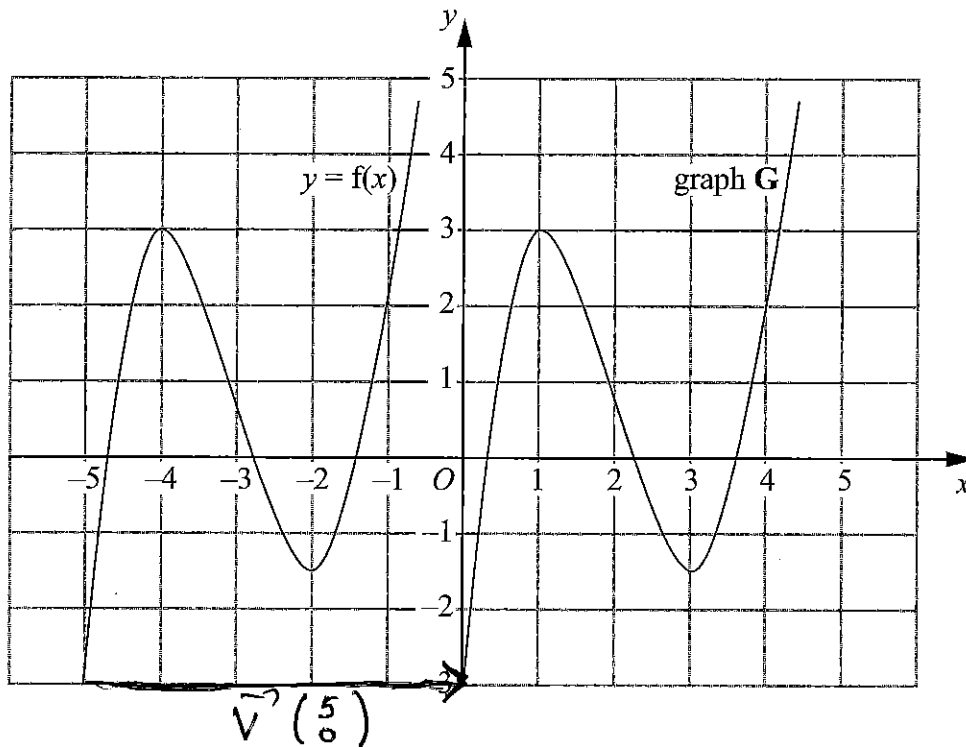
Area of segment = 1.771010

...........1.77........... cm²

Q26

(Total 5 marks)

27. The graph of $y = f(x)$ is shown on the grid.

$$V^{-7}\begin{pmatrix} 5 \\ 0 \end{pmatrix}$$

The graph **G** is a translation of the graph of $y = f(x)$.

(a) Write down, in terms of f, the equation of graph **G**.

Translation $V^{-7}\begin{pmatrix} 5 \\ 0 \end{pmatrix}$

$f(x) \longrightarrow f(x-5)$

$y = \underline{\quad f(x-5) \quad}$

(1)

The graph of $y = f(x)$ has a maximum point at $(-4, 3)$.

(b) Write down the coordinates of the maximum point of the graph of $y = f(-x)$.

$f(x) \longrightarrow f(-x)$.

$(-4, 3) \longrightarrow (--4, 3)$

$(4, 3)$

($\underline{\quad 4 \quad}$, $\underline{\quad 3 \quad}$)

(2)

Q27

(Total 3 marks)

TOTAL FOR PAPER: 100 MARKS

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