

# Grade C Revision Passport

## MR BARTON'S SOLUTIONS

Mean from a  
Grouped Table

Foot Length	FREQ	MP	MP × Freq
$5 < L \leq 10$	5	7.5	37.5
$10 < L \leq 15$	17	12.5	212.5
$15 < L \leq 20$	8	17.5	140
	<u>30</u>		<u>390</u>

a) Median =  $\frac{30 + 1}{2} = 15.5$ th person

They would be in the 2nd group ( $10 < L \leq 15$ )  
we could use Linear Interpolation to find a  
specific value:

They would be the 10.5th person in that group  
The group is 5 wide

$$\rightarrow \text{Median} = 10 + \left(\frac{10.5}{17}\right) \times 5 = 13.088... \text{ cm}$$

↑

Don't worry too much  
about this!

b) Mean.

Need midpoint (MP) and Midpoint × Freq column

$$\text{Mean} = \frac{\text{Sum of MP} \times \text{Freq}}{\text{Total Freq}} = \frac{390}{30} = \underline{\underline{13 \text{ cm}}}$$

# Sequences

a) 7, 11, 15, 19, 23

$\underbrace{\quad}_4 \quad \underbrace{\quad}_4 \quad \underbrace{\quad}_4 \quad \underbrace{\quad}_4$

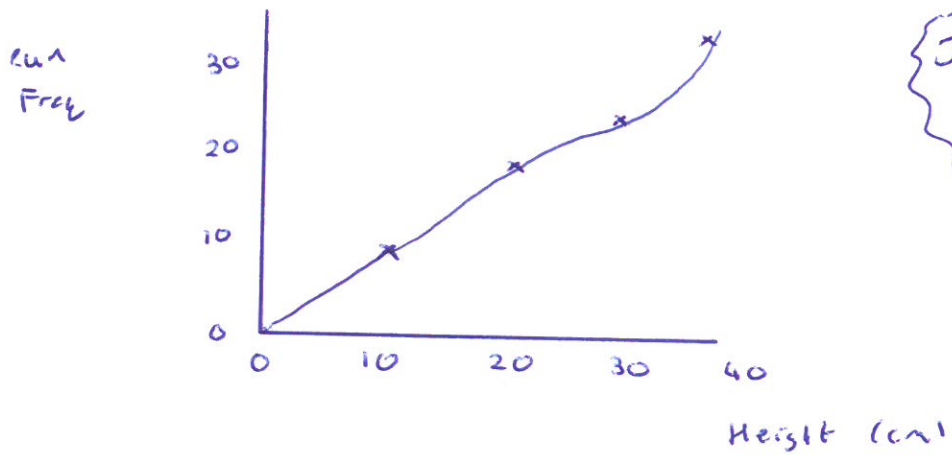
(4n) 4    8    12    16    20    →    4n + 3

b) 20th term :    4(20) + 3  
                       = 80 + 3            = 83

## Cumulative Frequency

Height	Freq	Cum Freq
$0 < h \leq 10$	7	7
$10 < h \leq 20$	8	15
$20 < h \leq 30$	6	21
$30 < h \leq 40$	9	30

Plot cumulative frequency v upper group boundary



Join with smooth curve

# Estimation

Round to 1 sig fig!

$$a) \frac{2.4 \times 296.3}{(2.37)^2} = \frac{2 \times 300}{2^2} = \frac{600}{4} = 150$$

b) Estimate:  $1240 \approx 1000$   
 $10.8p \approx 10p$   
 $1000 \times 10p = 10,000p = \pounds 100$   
 So she is about right

Exactly:  $1240 \times 10.8$   
 $= 124 \times 108$

	100	20	4
100	10000	2000	400
8	800	160	32

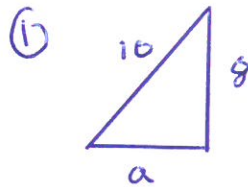
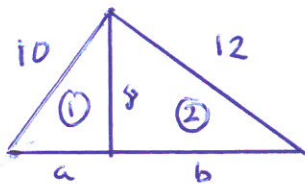
$$\begin{array}{r} 10000 \\ 2000 \\ 800 \\ 400 \\ 160 \\ 32 \\ \hline 13392 \end{array}$$

$$= 13,392p$$

$$= \pounds 133.92$$

So  $\pounds 100$  is not enough.

# Pythagoras



$$\sqrt{10^2 - 8^2} = a$$

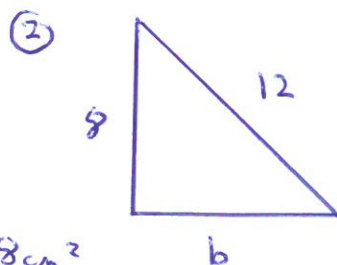
$$\sqrt{100 - 64} = a$$

$$\sqrt{36} = a$$

$$\rightarrow a = 6 \text{ cm}$$

$$\text{base} = 6 + 8.944$$

$$= 14.944$$



$$b = \sqrt{12^2 - 8^2}$$

$$= \sqrt{144 - 64}$$

$$= \sqrt{80}$$

$$= 8.944 \dots \text{ cm}$$

$$\text{Area} = \frac{b \times h}{2}$$

$$= \frac{14.944 \times 8}{2} = 59.8 \text{ cm}^2$$

(10p)

## Best Buy

$$\begin{aligned} 5 \text{ doughnuts} &= \text{\$} 3.35 \\ \rightarrow 10 \text{ doughnuts} &= \text{\$} 7.70 \end{aligned}$$

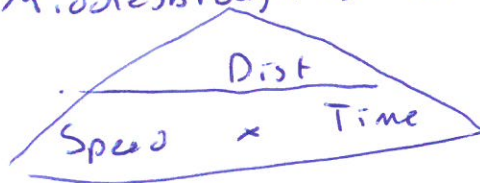
$$\begin{aligned} 2 \text{ doughnuts} &= \text{\$} 1.38 \\ \rightarrow 10 \text{ doughnuts} &= \text{\$} 6.90 \end{aligned}$$

$\therefore$  2 doughnuts is cheaper

## Distance Charts

a) I don't think there is enough info  $\ddot{\smile}$

b) Middlesbrough  $\rightarrow$  York = 45 miles



$$\text{Time} = \frac{\text{Distance}}{\text{Speed}}$$

$$= \frac{45}{60} = \frac{3}{4} \text{ hour}$$

$$= 45 \text{ mins}$$

## Equations

$$a) 18 + 6x = 2x + 42$$

$$\begin{array}{r} -2x \\ -18 \\ \hline \div 4 \end{array} \left\{ \begin{array}{l} 18 + 4x = 42 \\ 4x = 24 \\ x = 6 \end{array} \right.$$

$$b) 12 - 3x = 5x + 30$$

$$\begin{array}{r} +3x \\ -30 \\ \hline \div 8 \end{array} \left\{ \begin{array}{l} 12 = 8x + 30 \\ -18 = 8x \\ -\frac{18}{8} = x \end{array} \right.$$

$$\rightarrow x = -\frac{9}{4} \text{ or } -2.25$$

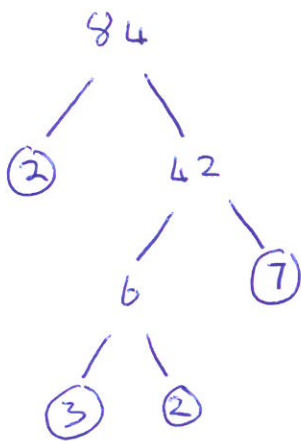
Circles

Area of square =  $15 \times 15 = 225 \text{ cm}^2$

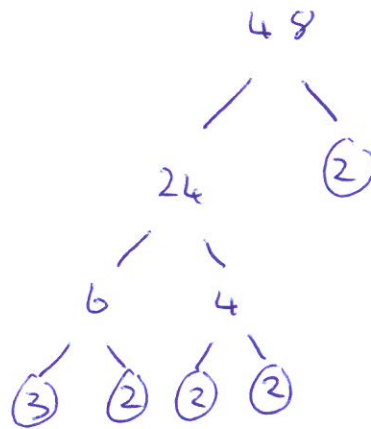
Area of circle =  $\pi r^2$   
 $= \pi \times 7.5^2 = 176.714... \text{ cm}^2$

Area of shaded region =  $225 - 176.714...$   
 $= 48.3 \text{ cm}^2$  (1dp)

HCF & LCM



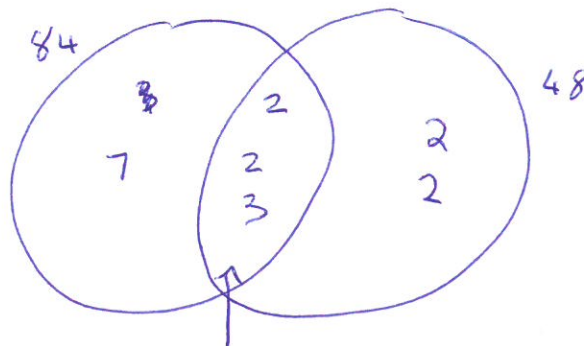
$84 = 2 \times 2 \times 3 \times 7$   
 $= 2^2 \times 3 \times 7$



$48 = 2 \times 2 \times 2$   
 $\times 2 \times 3$   
 $= 2^4 \times 3$

$84 = 2 \times 2 \times 3 \times 7$

$48 = 2 \times 2 \times 2 \times 2 \times 3$



LCM  
 $= 7 \times 2 \times 2 \times 3 \times 2 \times 2$   
 $= \underline{\underline{336}}$

HCF =  $2 \times 2 \times 3$   
 $= \underline{\underline{12}}$

## Ratio

Red : Blue

$$\frac{28}{3} \times \left( \begin{array}{l} 3 : 4 \\ 28 : \square \end{array} \right) \times \frac{28}{3}$$
$$\underline{\underline{37\frac{1}{3} L}}$$

Possibly a mistake in the question.

Maybe it is 28L of Blue, in which case:

Red : Blue

$$\times 7 \left( \begin{array}{l} 3 : 4 \\ \square : 28 \end{array} \right) \times 7$$
$$\underline{\underline{21L}}$$

## Form & Solve Equations

Angles in a quadrilateral add to  $360^\circ$

$$\rightarrow 90 + x - 10 + x + 20 + 2x - 60 = 360$$

$$\rightarrow 4x + 40 = 360$$

$$\begin{array}{l} -40 \\ \hline \div 4 \end{array} \left\{ \begin{array}{l} 4x \\ x = \underline{\underline{80^\circ}} \end{array} \right. = 320$$

## Scatter Graphs

- Positive Correlation
- On my sheet!
- I got about 42 kg

## Percentage Increase or Decrease

CALC 1

$$8.80 \times 0.85 \\ = \pounds 7.48$$

CALC 2

$$9.90 \times 0.74 \\ = \pounds 7.33 \text{ (2dp)}$$

CALC 2 is cheaper

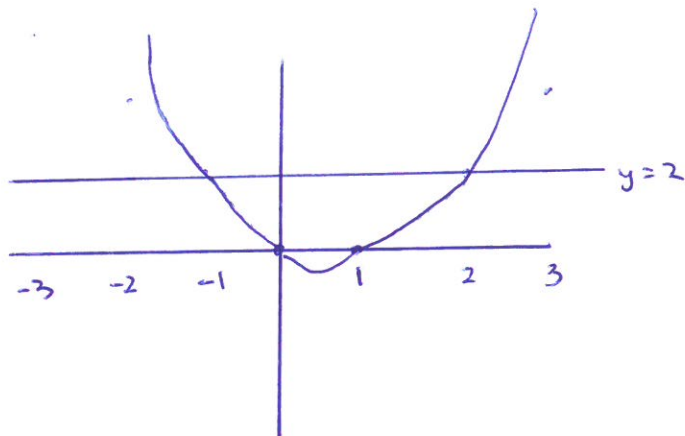
## Quadratic Graphs

a)  $y = x^2 - x$

$x$	-3	-2	-1	0	1	2	3
$y$	12	6	2	0	0	2	6

b)

①



c)  $x^2 - x = 2$

$\rightarrow x = 2$

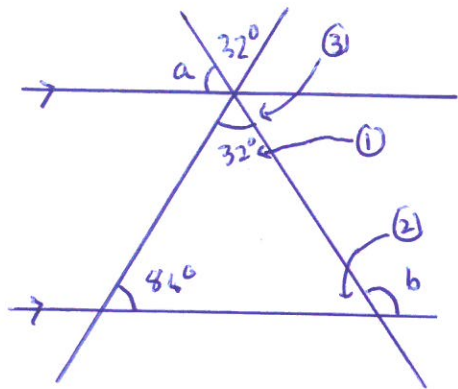
$x = -1$

## Pie chart

<u>No. People</u>	<u>Sweet</u>	<u>Size of Angle</u>
26	Naribo	$78^\circ$
48	Minstrels	$144^\circ$
46	M & Ms	$138^\circ$

120 people  
 $\rightarrow \frac{360}{120} = 3^\circ$   
 per person

# Angles on Parallel Lines



① Vertically opposite angles are equal

② =  $64^\circ$

Angles in a triangle add to  $180^\circ$

$b = 180 - 64^\circ = 116^\circ$

Angles on a straight line equal  $180^\circ$

③ =  $64^\circ$

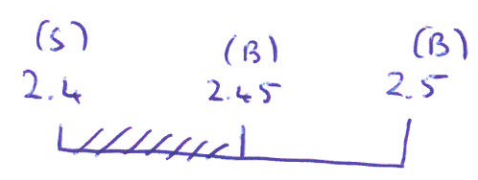
Supplementary angles add to  $180^\circ$

$a = 64^\circ$  vertically opposite angles are equal.

## Trial & Improvement

$x^3 + 4x = 24$

$x$	$x^3 + 4x$	Big/Small
2	16	Small
3	39	Big
2.5	<del>23.125</del> 25.625	Small Big
2.4	23.424	Small
2.45	24.506	Big



→  $x = 2.4$  (1dp)