

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Pages	Mark
3	
4 - 5	
6 - 7	
8 - 9	
10 - 11	
12 - 13	
14 - 15	
TOTAL	



Level 2 Certificate in Further Mathematics

Further Mathematics

Level 2

8360/1

Practice Paper Set 3

Paper 1

Non-Calculator

<p>For this paper you must have:</p> <ul style="list-style-type: none"> mathematical instruments. <p>You may not use a calculator.</p>	
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Time allowed

1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the space provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- In all calculations, show clearly how you work out your answer.

Information

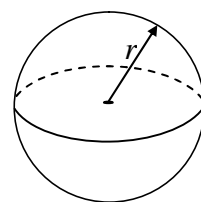
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 70.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer booklet.

8360/1

Formulae Sheet

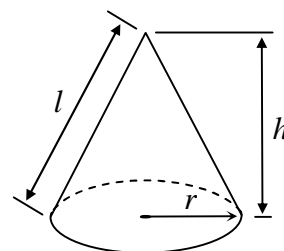
$$\text{Volume of sphere} = \frac{4}{3} \pi r^3$$

$$\text{Surface area of sphere} = 4\pi r^2$$



$$\text{Volume of cone} = \frac{1}{3} \pi r^2 h$$

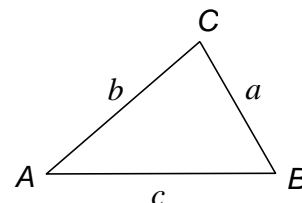
$$\text{Curved surface area of cone} = \pi r l$$



In any triangle ABC

$$\text{Area of triangle} = \frac{1}{2} ab \sin C$$

$$\text{Sine rule} \quad \frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$



$$\text{Cosine rule} \quad a^2 = b^2 + c^2 - 2bc \cos A$$

$$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$$

The Quadratic Equation

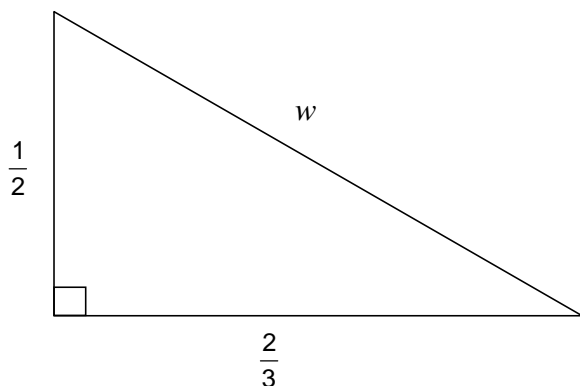
The solutions of $ax^2 + bx + c = 0$, where $a \neq 0$, are given by $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

Trigonometric Identities

$$\tan \theta \equiv \frac{\sin \theta}{\cos \theta} \quad \sin^2 \theta + \cos^2 \theta \equiv 1$$

Answer **all** questions in the spaces provided.

1 Work out the exact value of w .



Not drawn accurately

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$w =$ (4 marks)

2 $5(3x - 2) - 3(x - h) \equiv 4(kx + 2)$

Work out the values of h and k .

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$h =$, $k =$ (4 marks)

3 Solve $\frac{y-2}{5} + \frac{2y+1}{4} = 3$

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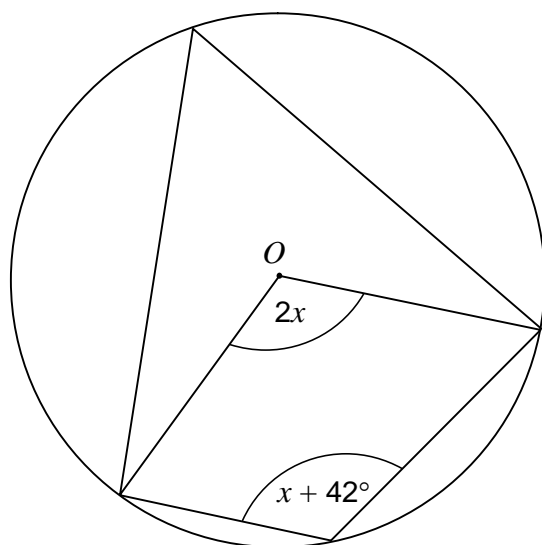
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$y = \dots\dots\dots$ (4 marks)

4 O is the centre of this circle.



Not drawn
accurately

Work out the value of x .

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$x = \dots\dots\dots$ degrees (3 marks)

5 Simplify fully $20a^9b^6 \div 4a^3b^2$

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Answer (2 marks)

6 The matrix $\begin{pmatrix} a & b \\ -a & 2b \end{pmatrix}$ maps the point (5, 4) onto the point (1, 17).

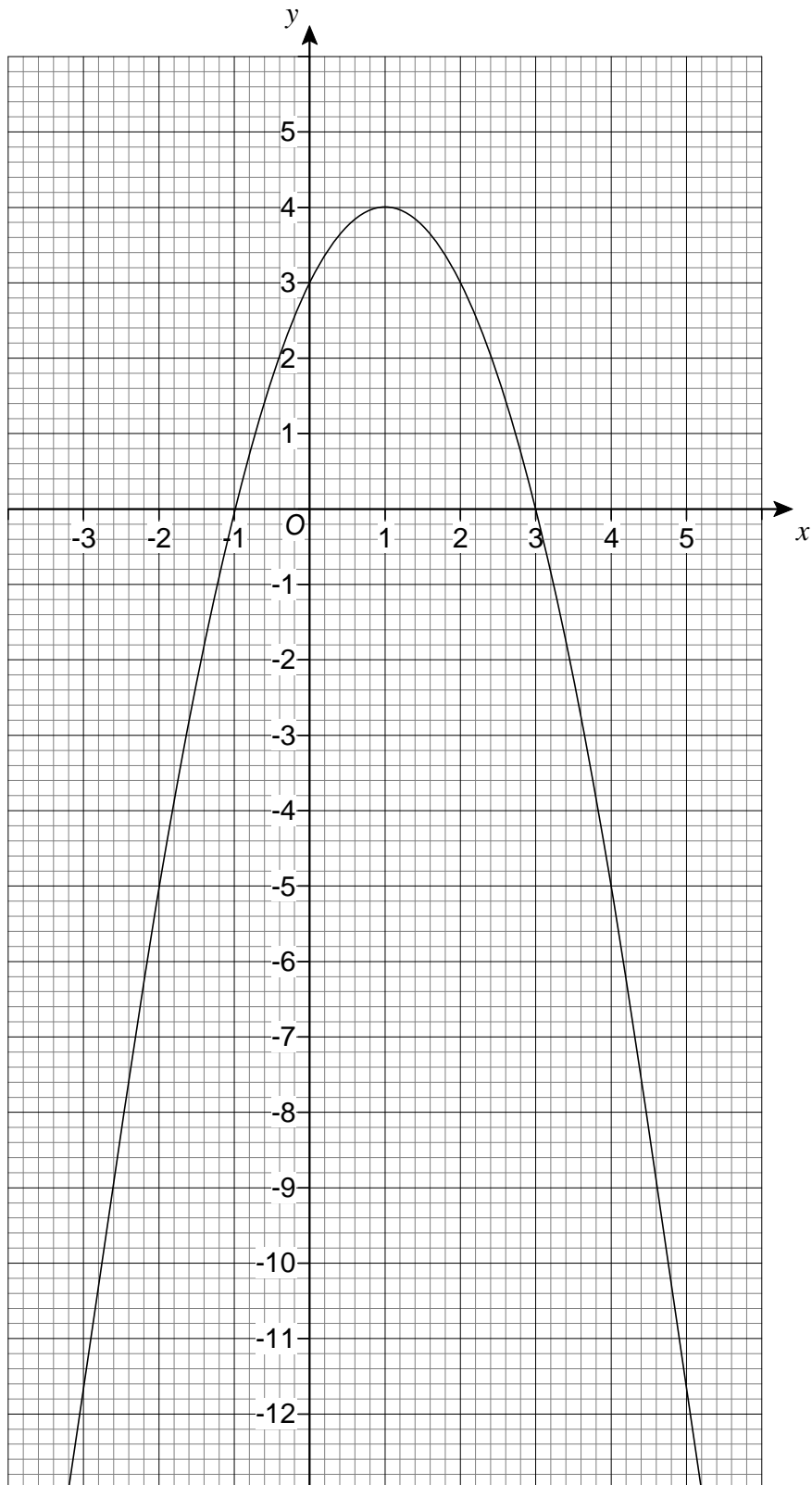
Work out the values of a and b .

$a = \dots\dots\dots$, $b = \dots\dots\dots$ (5 marks)

7

$f(x)$ is a quadratic function with domain all real values of x .

Part of the graph of $y = f(x)$ is shown.



7 (a) Write down the range of $f(x)$.

Answer (1 mark)

7 (b) Use the graph to find solutions of the equation $f(x) = 1$
Give your solutions to one decimal place.

Answer (2 marks)

7 (c) Use the graph to solve $f(x) < 0$

Answer (2 marks)

8 $x^{\frac{1}{2}} = 6$ and $y^{-3} = 64$

Work out the value of $\frac{x}{y}$

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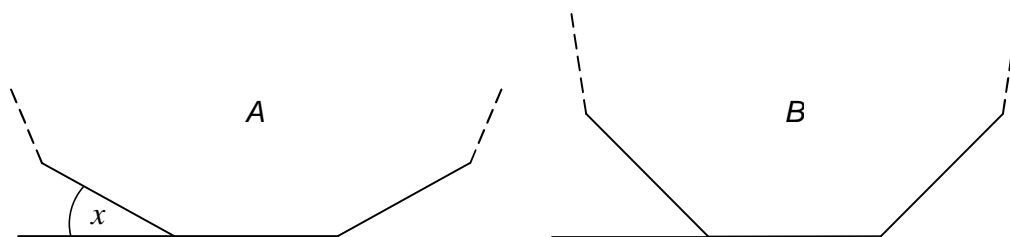
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Answer (4 marks)

- 9 A and B are regular polygons.
An exterior angle of A is x .

Not drawn accurately



Here is some information about them.

	$A : B$
Ratio of exterior angles	1 : 3
Ratio of interior angles	7 : 6

- 9 (a) Write down an expression in x for an exterior angle of polygon B .

Answer (1 mark)

- 9 (b) Prove that polygon A has 30 sides.

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(5 marks)

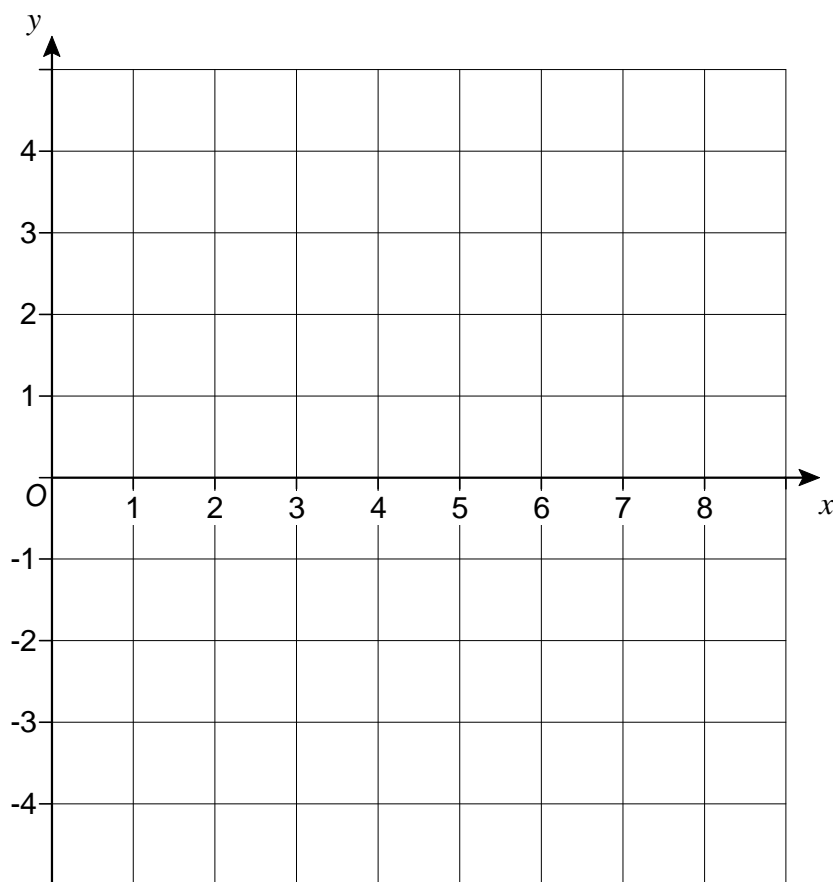
10 $y = f(x)$ is a continuous graph.

When $0 \leq x < 3$ $\frac{dy}{dx} = 2$ and this part of the graph passes through $(2, 1)$.

When $3 \leq x < 5$ $\frac{dy}{dx} = 0$

When $5 \leq x \leq 8$ $\frac{dy}{dx} = -1$

Draw the graph of $y = f(x)$ for $0 \leq x \leq 8$



(3 marks)

Turn over for the next question

11 Angle θ is obtuse and $\sin \theta = \frac{\sqrt{5}}{3}$

Work out the values of $\cos \theta$.

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$\cos \theta =$ (4 marks)

12 (a) $(x + 3)$ is a factor of $x^3 + 6x^2 + ax - 12$

Show that the value of a is 5

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(2 marks)

12 (b) Hence, factorise fully $x^3 + 6x^2 + 5x - 12$

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$(x + 3)$ (.....) (.....) (3 marks)

Turn over for the next question

- 13 Expand and simplify $(\sqrt{5} + 3)(\sqrt{5} - 2)(\sqrt{5} + 1)$

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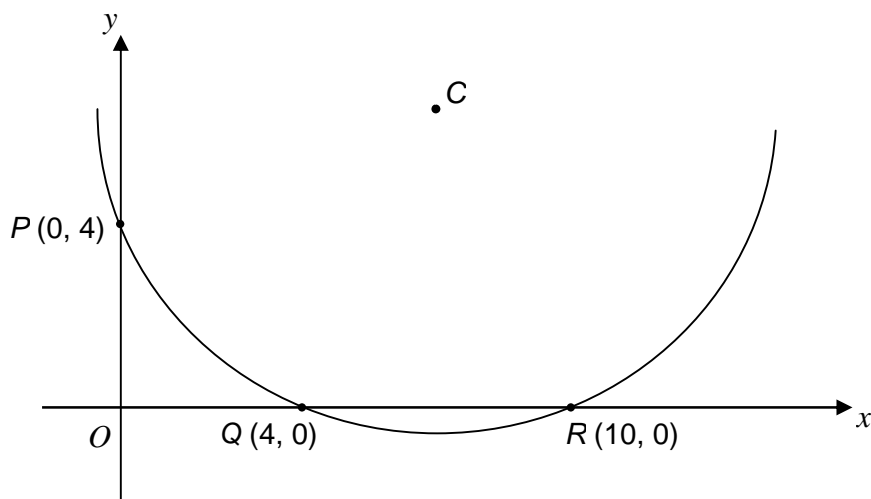
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Answer (4 marks)

- 14 The sketch shows part of a circle, centre C , that intersects the axes at points P , Q and R .



- 14 (a) Explain why the centre of the circle lies on the line $x = 7$.

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(1 mark)

14 (b) Show that the line $y = x$ is the perpendicular bisector of the line PQ .

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(2 marks)

14 (c) Work out the equation of the circle.

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Answer (4 marks)

Turn over for the next question

15 $2x^2 - 4x + 5 \equiv a(x + b)^2 + c$

Work out the values of a , b and c .

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$a = \dots\dots\dots, b = \dots\dots\dots, c = \dots\dots\dots$ (4 marks)

16 A curve has equation $y = 4x^3 + 6x^2 + 3x + 5$

Work out the coordinates of any stationary points on this curve and determine their nature.

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Answer (6 marks)

END OF QUESTIONS

10

There are no questions printed on this page

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ANSWER IN THE SPACES PROVIDED**